# **RADAR SYSTEMS**

 EC812PE: RADAR SYSTEMS (PE – V) (ELECTIVE V) UNIT - 1A**B.TECH IV YEAR II SEMESTER** BY **Prof.G.KUMARASWAMY RAO** (Former Director DLRL Ministry of Defence) BIET

**Acknowledgements** The contents, figures, graphs etc., are taken from the following Text book & others **"INTRODUCTION TO RADAR SYSTEMS**" Merill I.Skolnik **Second Edition Tata Mcgraw – Hill publishing company Special indian edition** 

#### **TITANIC SHIP**



# **TITANIC SHIP**

- British largest passenger ship sank in North Atlantic on 15 April 1912 after colliding with Ice berg
- Broke, disintegrated water entered and the ship sank
- Maiden voyage from Southampton to New-york city
- Luxurious ship for wealthy people . Swimming pools, libraries, high class restaurants , gymnasiums etc
- 1500 died in the cold water
- Worst deadliest disaster

# **CYLONES**



# BATS

To echolocate, bats send out sound waves from the mouth or nose. When the sound waves hit an object they produce echoes The wavelength of a 34 kHz note (which is what the Free-tailed Bat *Tadarida brasiliensis* uses), is a mere 1 cm



#### AIR PORT AIR TRAFFIC CONTROL DISPLAY



## **RADAR INVENTION LINKED TO WORLD WARS**

- World war I: 1914 to 1918
- France , UK, Russia Vs Germany, Austria, Hungary, Italy
- Casualities : 4 Crores of population equivalent to Population of Telengana
- World War II : 1939 to 1944
- Britain, France , Austria , Canada, Soviet Union , USA

#### Vs

- Germany, Italy, Japan
- Casualities : 8.5 crores Population

#### **SYLLABUS**

# EC812PE: RADAR SYSTEMS (PE – V) ELECTIVE-V B.TECH IV YEAR II SEMESTER UNIT I

- Basics of Radar: Introduction, Maximum Unambiguous Range, Simple form of Radar Equation, Radar Block Diagram and Operation, Radar Frequencies and Applications, Prediction of Range Performance, Minimum Detectable Signal, Receiver Noise, Modified Radar Range Equation, Illustrative Problems.
- Radar Equation: SNR, Envelope Detector False Alarm Time and Probability, Integration of Radar Pulses, Radar Cross Section of Targets (simple targets – sphere, cone-sphere), Transmitter Power, PRF and Range Ambiguities, System Losses (qualitative treatment), Illustrative Problems.

# **RADAR** is Acronym for <u>**RA</u>dio <u>D</u>etection <u>And Ranging</u></u>**

## **BASICS OF RADAR**

#### > What is a RADAR?

RADAR is an Electromagnetic system doing the

following functions.

- (i) Detects the presence of reflective object
- (ii) Gives the Range of the reflective object
- (iii) Locates the reflective object in angle (azimuth & elevation)
- (iv) Gives the Radial velocity of moving object

#### **BASICS OF RADAR**

#### > What is a RADAR? Simpler definition

RADAR is a detection system that uses radio waves to determine the distance (ranging), angle , and velocity of objects

# **Basics Of Radar (contd...)**

- What are the Reflective objects (with high die-electric constant like Aluminum and its alloys)
  - (i) Aircraft (ii) Ship (iii) Missile (iv) Motor Vehicle etc.
- The Reflective object is called TARGET
- In fact all objects reflect EM energy to some extent, some more, some less.

#### **RADAR Vs HUMAN EYE**



#### Radar Advantages and Disadvantages

## **Advantages of Radar over Human eye:**

- (i) Radar detects and locate targets hundreds of Kms. away.
- (ii) Radar detects targets in darkness, rain, snow, haze, smoke etc. where human eye fails.

#### **Disadvantages of Radar:**

- (i) Resolution is poor compared to eye.
- (ii) Cannot discriminate colours.
- Infra Red also can detect targets but it is heavily attenuated in snow, rain and haze.



## **Pulse Radar Operation**

#### **PRINCIPLE OF RADAR**

- Metallic surfaces reflect E.M. (Electro Magnetic) energy (known in early 18<sup>th</sup> century)
- Principle of Radar:
- (i) E.M. energy radiated into space
- When a metallic or high dielectric constant object say aircraft or ship comes in its path, a portion of energy is reflected.
- (iii) The reflected energy is called ECHO. Echo indicates presence of target.
- (iv) Echo is detected in a high sensitive receiver called Radar Receiver.
- (v) Echo is amplified and shown visually on a Radar display.



## **Radar Target Discriminants**

# PHOTOGRAPHS OF A FEW EXISTING RADARS

#### **Surveillance and Fire Control Radars**

Courtesy of Raytheon. Used with permission.

Courtesy of Raytheon. Used with permission.





Courtesy of Raytheon. Used with permission.

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Courtesy of Raytheon. Used with permission.



Courtesy of US Navy.

#### **Airborne and Air Traffic Control Radars**







## **Early Warning Radar System**



#### **Radar System**







## **TTR with Acquisition**

















Diagram of a typical 3D-Radar, a mix of vertical electronic beam steering and horizontal movement of a pencil-beam



#### SWORD FISH RADAR

#### **FLY CATCHER RADAR**



#### **TARGET DETECTION BEFORE RADAR**

#### PRE RADAR AIRCRAFT DETECTION

 Before World war II (1939-44) locating aircraft was done by Sound Locators. Maximum Detection range was 20 miles (32.1 Kms)
#### **Pre-Radar Aircraft Detection – Optical Systems**



Significant range limitation

- Attenuation by atmosphere
- Narrow field of view
  - Caused by very small wavelength
- Clouds Cover limits operational usefulness
  - Worldwide 40-80% of the time



Courtesy of UK Government



Courtesy of National Archives.

#### **Pre-Radar Aircraft Detection – Acoustic Systems**

#### Japanese Acoustic Detection System



Courtesy of Wikimedia

- Developed and used in first half of 20<sup>th</sup> century
- Attributes
  - Limited Range approximately 10+ miles
  - Limited field of view
  - Ambient background noise limited (weather, etc)
- Used with searchlights at night

#### **US Acoustic Detection Systems**





Courtesy of US Army Signal Corps.

## HISTORICAL BACKGROUND OF RADAR DEVELOPMENTS

#### **HISTORICAL BACKGROUND OF RADAR DEVELOPMENTS**

- 1886 -Henrich Hertz demonstrated the similarity between Radio waves and light waves
  - He showed Radio waves could be reflected by metallic and dielectric objects
  - He performed experiment with short waves ie., 66 cms wavelength (454 MHz)
    Later Experiments were all on long wave lengths (low frequencies) until late 1930s
- 1903 Hullsmeyer (German scientist) showed that Radio waves reflected from ships
  - Not much interest was shown by German Navy then

- 1922 Marconi predicted Radio waves could be reflected back from a ship or steamer.
- Receiver could capture and reveal the presence and bearing of the ship in fog or thick weather
- 1922 A.H. Taylor and L.C. Young (National Research lab NRL) detected a wooden ship using CW wave Interference Radar (uses Doppler principle)
  - They used a separate transmitter and receiver (Bi-static Radar) Wave length 5 Mts (60 MHz.)

- 1925 Breit and Tuve used the pulse technique for measuring the height of the lonosphere
- 1930 L.A. Hyland working with Direction finding apparatus found whenever an aircraft crossed the transmitted beam of 33 MHz, an increase in the received signal frequency was observed
- Principle of CW Interference Radar:

Because of Doppler effect there was an interference produced between the direct signal of the transmitter and the doppler frequency shifted signal reflected by a moving target. This effect is called CW wave interference

- 1933 Taylor, Young and Hyland took a patent on a Pulse "System for detecting objects by Radio" using principle of CW Wave Interference
- CW Transmission does not give Range of the target They give only the presence or absence of a target
- 1934 R.M. Page made efforts to get position information using Pulse transmission
- 1936 At NRL 28.3 MHz., with pulse width of 5 Micro sec. practical Pulse radar was experimented.
   Range obtained was 25 Miles (40.2 Kms)

- 1938 200 MHz. Pulse Radar was installed on Destroyer ship LEART. Power transmitted 6 KW Range 50 Miles (80.5 Kms)
- 1941 SCR 270/271 Early warning Radars produced in large numbers.
   SCR 268 was tracking radar, used in gun firing at enemy aircraft.
- 1941 Attack on Pearl harbour was detected by this Radar. Unfortunately the significance of blips were not realised until after the bombs were dropped
- **1944** SCR 584, most significant tracking radar controlled a battery of 4 anti aircraft guns.

#### World War 2 Air Defense System



Courtesy of US Army

#### **BRITISH RADAR DEVELOPMENTS**

- 1935 12 MHz. Pulse Radar obtained 40 Miles (64.3 Kms) range
- 1937 April CH (Chain Home ) Radar were demonstrated. Played the most crucial role in defeat of German Aircrafts over London. Sir. Robert Watson was the Chief Architect of this Radar

### **British Radar Developments (contd.)**

- 1939 Aircraft Interception Radar mounted on aircraft at 200 MHz. was developed. It detected aircrafts, surface ships and submarines
- 1940 after this year developments carried out jointly by US and Britain
- For better angular resolution and smaller size antenna higher frequency ie at microwave is necessary
- 1940 Cavity Magnetron was developed. Tube was developed by Randell and Boot. It is a cavity backed microwave tube operating at 10cms (3GHz) and output of 1 KW. (First Microwave Radar) This gave the necessary thrust to further Radar developments

#### Properties of Waves Phase and Amplitude



# Polarization



The relative value of two things, measured on a logarithmic scale, is often expressed in deciBel's (dB)



#### Isotropic antenna

#### **Directional antenna**







# **Scientific Notation and Greek Prefixes**

Scientific Notation	Standard Notation	Greek Prefix	Radar Examples
<b>10</b> <sup>9</sup>	1,000,000,000	Giga	GHz
<b>10</b> <sup>6</sup>	1,000,000	Mega	MHz, MW
<b>10</b> <sup>3</sup>	1,000	kilo	km
10 <sup>1</sup>	10	-	-
<b>10</b> <sup>0</sup>	1	-	-
<b>10</b> -3	0.001	milli	msec
<b>10</b> -6	0.000,001	micro	μsec

MHz = Megahertz MW = Megawatt



**Courtesy Berkeley National Laboratory** 

Radar Frequencies aswamy RAO BIET



#### IEEE Standard Radar Bands (Typical Use)

HF	3 – 30 MHz		
VHF	30 MHz–300 MHz	Search	
UHF	300 MHz–1 GHz	Radars	
L-Band	1 GHz–2 GHz		
S-Band	2 GHz–4 GHz	Search & Track Radars	
C-Band	4 GHz–8 GHz		
X-Band	8 GHz–12 GHz	Imaging Radars	
Ku-Band	12 GHz–18 GHz		
K-Band	18 GHz–27 GHz	Missile	
Ka-Band	27 GHz–40 GHz	Seekers	
W-Band	40 GHz – 100+ GHz 🔸		

- For mounting on ships and aircrafts smaller antennas are required. To achieve this one need to use higher frequencies ie lower wave lengths.
- However technology to make components at higher frequencies were not available at that point in time.
- Antenna size is directly proportional to the wave length and indirectly proportional to frequency ( $\lambda$  =C/f)

Frequency	Wave length	Frequency	Wave length
20 MHz	15 Mts	1 GHz(1000 MHz)	0.3 Mts
60 MHz	5 Mts	2 GHz	0.15 Mts
200 MHz	1.5 Mts	4 GHZ	0.075 Mts
600 MHz	0.5 Mts	10 GHz	0.03 Mts(3 Cms)

# **The Early Days of Radar**

- Sir Robert Watson-Watt
  - Considered by many "the inventor of radar"
  - Significant early work occurred in many other countries, including the United States (1920sand 1930s)
  - After experimental verification of the principles, Watson-Watt was granted a patent in 1935
  - Leader in the development of the Chain Home radar systems Chain Home, Chain Home Low Ground Control Intercept and Airborne Intercept Radar
- Tizard Mission
- MIT Radiation Laboratory





Courtesy of Wikimedia

### Chain Home Radar System

#### **Typical Chain Home Radar Site**



#### Chain Home Radar Parameters

- Wavelength
  - 10 to 15 m
- Frequency – 20 to 30 MHz
- Antenna
  - Dipole Array on Transmit
  - Crossed Dipoles on Receive
- Azimuth Beamwidth

   ~ 100°
- Peak Power
  - 350 kW
- Detection Range
  - ~160 nmi on JU-88 German Bomber

#### **Chain Home Transmit & Receive Antennas**



#### **Chain Home Radar Operations**



#### **Operation Room at Air Group 10**



#### Radar and "The Battle of Britain"

#### Approximate Chain Home Radar Coverage Sept 1940 (21 Early Warning Radar Sites)



- The Chain Home Radar
  - British "Force Multiplier" during the Battle of Britain"
- Timely warning of direction and size of German aircraft attacks allowed British to
  - Focus their limited numbers of interceptor aircraft
  - Achieve numerical parity with the attacking German aircraft
- Effect on the War
  - Germany was unable to achieve Air Superiority
  - Invasion of Great Britain was postponed indefinitely

#### Utility and Positive Attributes of Radar

- Long range detection and tracking of targets
  - 1000's of miles
- All weather and day/night operation
- Wide area search capability
- Coherent operation enables
  - Simultaneous reliable target detection and rejection of unwanted "clutter" objects
  - Target imaging (fixed and moving)
  - Very fast beam movement with electronic scanning of antennas (microseconds)
  - Ability to adaptively shape antenna beam to mitigate interference and jamming
- "Relatively lossless, straight line propagation at microwave frequencies

### Negative Attributes / Challenges of Radar

- Long range detection requires
  - Large and heavy antennas
  - High power transmitters
  - Significant power usage
  - \$\$\$\$\$
- Radar beams not propagate well
  - through the Earth, water, or heavy foliage
  - around obstacles
- Vulnerable to jamming, and anti-radiation missiles
- Target can detect that it is being illuminated
- Target can locate the radar in angle-space
- The echo from some targets is becoming very small
  - Low observable technology

### **TECHNOLOGIES USED IN RADAR**

- Radar is an Engineering system and integrates many of following technologies.
  - (i) Microwaves Engineering
  - (ii) Antenna Technology
  - (iii) R.F. Plumbing
  - (iv) High Power Microwave Transmitter
  - (v) High Sensitivity Microwave Receiver
  - (vi) I.F. Circuit
  - (vii) Matched Filter
  - (viii) Signal Processing
    - (ix) Display Technology
  - (x) Control Systems

## **FUNCTIONS OF RADAR**

- **1. Detect the presence of target**
- 2. Gives the range of the target from the Radar station
- 3. Gives the azimuth angle and elevation angle of the target
- 4. Gives the radial velocity of target.

### **PRINCIPLE OF RADAR**



## Principle Of Radar (Contd..)

- 1. Transmitter generates a high power Pulse modulated sine wave.
- 2. T/R switch connects Antenna to  $T_x$
- 3. Antenna converts Electrical Pulse to EM Wave and transmits in space.
- 4. T/R switch now connect Antenna to  $R_x$
- 5. Aircraft reflects a portion of EM energy called Echo.
- 6. Echo collected by Antenna converts EM pulse to RF Pulse.
- 7. Signal Processor converts RF Pulse to video pulse after amplification.
- 8. Display shows visually the Echo.

### **SUBSYSTEMS OF RADAR**

1. Transmitter: This generates the Electrical energy at R.F.(Radio Frequency). This may be a power oscillator or a power amplifier.

- 2. Antenna: This is a transducer which converts the RF electrical signals to EM signals and transmits in space.
- It also function as a receiving antenna and converts EM signal to Electrical signal.

### Subsystems of Radar(contd...)

- **3.Receiver:** The weak Echo is amplified and processed to detect presence of target.
- This consists of Signal Processing Circuits to optimize the signal to Noise ratio.
- The R.F. Echo is envelope detected to obtain Video and amplified to suit the Display requirements.
- 4.Display: Presence and location of a target is displayed on a CRT usually called the PPI (Plan Position Indicator).
- The dot (spot) on the CRT gives out the target coordinates i.e. Range, Azimuth & Elevation.

### **Radar Principles**



#### **Radar Principles**



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### WHERE DO YOU USE RADAR

**1.Defence:** Detection and location of military (i) Aircrafts (ii)Ships (iii)Tanks (iv) Missiles **2.Civilian: (i)** Air Traffic Control(ATC) (ii) Ships Navigation (iii) Collision Avoidance **3.Meterology:** Weather prediction(storms & cyclones) 4.Remote Sensing: (i)Imaging (ii)Ground Mapping (iii)Agricultural Crop Monitoring **5.Police:** Speed monitiring & Control

### **APPLICATIONS OF RADAR**

- Radar has been employed on
- (i) Ground: To detect, locate and track aircraft or space targets.
- (ii) Sea: To navigate in sea or ocean in bad weather. Navigate safely in harbour and dock in the allotted berth without collision with other ships
- (iii) Air: (1) To detect other aircrafts, ships or land vehicles, (2) To avoid storms (3) terrain avoidance (4) Navigate from one air port to another.
- (iv) Space: (1) Guidance of Spacecraft, (2) Remote sensing of planets.

**1. AIR TRAFFIC CONTROL (ATC):** 

- Safely controlling aircraft traffic enroute airports.
- Controlling air traffic in the vicinity of airport when the density of aircraft trying to land on runway and take-off from runway is heavy.
- Radar is a part of Ground Control Approach (GCA) systems or ATC Radar Beacon System which guide aircrafts to a safe landing or take-off in bad weather.

### **2. AIRCRAFT NAVIGATION:**

- Radar mounted on aircraft gives a visual picture of weather conditions to the pilot in front of the moving aircraft. Regions of precipitation, heavy storm, clouds etc. shown by the radar enable pilot to steer the aircraft away from the danger regions.
- Radio Altimeter (FMCW Radar) gives the height of the aircraft from the ground.

#### **3. SHIP SAFETY:**

- Ships are mounted with Radars which warns the navigator about other ships in its vicinity especially in poor visibility conditions and avoid collisions.
- Ship radar facilitate the navigator for docking safely in the given berth in a harbour.
- Shore based Radars used for surveillance and navigation in a harbour and control the movement of ships in the harbour.

#### **4.REMOTE SENSING:**

- Radars are used for remote sensing of environment, like cyclones, storms, tornadoes etc.
- Radars are used for mapping the conditions of agricultural crops by sensing the water content in the plants. They are used in mapping forestry coverage and its density.
- Radars are used to probe moon and other geophysical objects like planets (radar astronomy) Radars are mounted on satellites or aircrafts for this purpose.
- Radars are used to detect and locate earth resources like water, ice cover, geological formations, environmental pollution, mapping sea conditions etc.
- Radars are used for satellite monitoring.

### 5. SPACE:

- Radars are mounted on space vehicles for rendezvous and docking, and for landing on planets like moon, mars etc.
- **6. LAW ENFORCEMENT:**
- Police Officers use Radars to measure the speed of automobiles like 4 wheelers, 2 wheelers on highway and avoid accidents due to over speeding
- Radars are used to detect intruding vehicles or persons in high security premises.

# APPLICATIONS OF RADAR (Contd..) 7. MILITARY:

- Radar is extensively used for military purposes.
- Long range surveillance of country's borders.
- Navigation of military aircraft and naval ships.
- Tracking hostile targets (aircraft or ships) and control the Anti aircraft Guns or control and guide missiles.

### **MILITARY RADARS**

### **Post World War–II Radars:**

- **1.N/SPY-1** Multifunction ship borne tactical Radar
- 2.AN/MPQ-53 Patriot Air Defence Radar
- 3.AN/FPS-108 COBRADANE Long Range Radar
- 4.AN/FPS-115 PAVE PAWS solid state early warning Radar

#### **DRDO Developed Radars:**

1.Indra I & II 2.Rajendra-Phased Array Radar for use with AKASH missile 3.Battle Field Surveillance Radar 4.Naval Maritime Radar



#### Radar-Directed AAA



#### Semi-Active Guidance (Mid-Course)

### **CONTINUED IN RADAR 1B**

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- Radar Equation: SNR, Envelope Detector False Alarm Time and Probability, Integration of Radar Pulses, Radar Cross Section of Targets (simple targets – sphere, cone-sphere), Transmitter Power, PRF and Range Ambiguities, System Losses (qualitative treatment), Illustrative Problems.



### INTRODUCTION

#### **PRINCIPLE OF RADAR**

- What are the basic functions of Radar? Explain
- Radar stands for Radio Detection And Ranging
- Basic functions of Radar are
- 1. Detect the object (also called target)
- 2. Calculate the Range of the target (Range of a target is the radial distance between the Radar antenna and target)
- Additional functions of Radar are
- 1. Give the direction of target. (By mounting the Radar antenna on a rotating servo pedestal, the azimuthal direction of target can be found out)

#### **PRINCIPLE OF RADAR (contd)**

- 2. Give the radial velocity of the target. (By using the Doppler principle, the radial velocity can be computed)
- PRINCIPLE OF RADAR:



#### **PRINCIPLE OF RADAR**



#### **PRINCIPLE OF RADAR (contd)**

1. The transmitting antenna transmits the electro-magnetic radiations in space for a short duration (pulsed). Its speed is that of light 3 x 10<sup>8</sup> meters/second. If an TRANSMITTING & RECEIVING ANTENNAL

object (also called target) is present



in the path of the EM pulse, it intercepts the radiation and backscatters the signal in all directions (omni). A portion of scattered signal reaches the radar antenna. The Receiving antenna captures the back-scattered radiation and applies it to the Radar Receiver. The receiver amplifies and processes the low energy signal and processes it. It measures the amount of time **TR** taken by the pulsed EM wave to reach the target and return back to the antenna.



#### **Pulse Modulation**

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#### **Pulse Mode Operation**





Radar systems classified according to specific function



#### Classification of radar sets according its use

#### **PULSE CHARACTERISTICS**

- Intub What are the desirable pulse characteristics and the factors that govern them Or Define a) PRF b) Unambiguous range
- There are 4 important pulse characteristics to be considered for the radar pulse
- 1. Carrier 2. Pulse width 3. Pulse repetition frequency – PRF
   4. Upambiguous Pango
  - 4. Unambiguous Range

#### **PULSE CHARACTERISTICS**

#### • 1. CARRIER:

The carrier used in a Radar is called the RF (Radio frequency) or Micro-wave signal. Their range may be from 3 MHzs to 300 MHzs. They are VHF, UHF, L,S,C,X,Ku,K,Ka bands and mm (millimetric) frequencies. High frequencies are used in Radar to keep the radar antenna within reasonable size

#### • 2. PULSE WIDTH:

In a Pulse radar the Carrier is modulated to get the range of the target. The Carrier is switched ON and OFF with the short duration pulse. The pulse width determines the dead zone of the range of the target. For example if the pulse width is 1 micro sec, detection of target range less than 150 meters is not possible. During the transmission of 1 micro sec high power pulse, the Radar receiver is blanked to protect it from damage because of high power transmission. Similarly if a pulse width of 10.8 micro sec is used there is no detection of target for 1 standard mile from the radar antenna

• 2. PULSE WIDTH (CONTD):

However in CW (Continuous Wave) radar no modulation is used. However the doppler principle is used to extract the radial velocity of the target

3. PULSE REPETITION FREQUENCY : (PRF)
 Pulse radar continuously transmits RF pulses
 continuously at a particular frequency. The echo
 (reflection) from the target is painted on the display by
 the Signal processor every time echo pulse is received
 PRF is the number of pulses transmitted in a second

$$PRF = \frac{1}{PRT (pulse repetition time)}$$

PRI (pulse repetition interval)

IPP(inter pulse period)

PRF is important because it determines the maximum target range R unambiguous and doppler velocity

- 4. MAX UNAMBIGUOUS RANGE (Runambiguous)
   It is the greatest range the transmitted can travel and comeback to the radar antenna before the transmission of next pulse
  - Echoes from target must arrive before the next pulse is transmitted to avoid Range Ambiguity
  - Echoes that arrive after the transmission of next pulse is transmitted are called Second Time around echoes. These second time around echoes give wrong reading of target range. They are interpreted as shorter target range than the actual.
  - There is a relation between PRF and (Runamb). Larger the PRF shorter is the (Runamb)
  - Max (Runamb) =  $\frac{C}{2 \text{ fp}}$  where  $f_p = PRF$  in HZs

➢ RF Sine wave (Between  $1G_{HZ}$  TO 40  $G_{HZ}$ ) modulated with a short pulse (Between 0.1 to 5 µ sec)

➢RF Pulse travels in air from Antenna to Target

Portion of EM energy is reflected after hitting the target (ECHO)

Echo reaches the same antenna



- T<sub>P</sub> Pulse Repetition Time
- T<sub>R</sub>– Time taken by EM pulse to travel to target and come back to same antenna – Elapsed Time between Transmission and Echo Pulse

$$f_P - Pulse Repetition frequency = \frac{1}{T_P}$$

- R Range of Target
- C Velocity of EM waves =  $3 \times 10^8$  Meters/sec
  - = 1.86 X 10<sup>5</sup> miles /sec

- The Range of the target from the Radar antenna is computed as follows
- Distance (Range) = Velocity X Time (elapsed between transmitted & received EM pulse)

• Range R= C x 
$$\frac{T_R}{2} = \frac{C TR}{2}$$

- where C = Velocity of EM waves and TR = elapsed between transmitted & received EM pulse
- 2 is used because the radiation travels twice the range before it reaches antenna

- If TR = 1 micro second R =  $\frac{3 \times 108 \times 1 \times 10 6}{100 \times 100}$  = 150 meters
- If TR = 10.8 micro second and c= 1,86,000 miles per sec  $\frac{186000 \times 10.8 \times 10 - 6}{1000} = 1$  mile (standard) R =

2

Distance= Velocity x Time taken  $2 R = C x T_R$   $R = C x T_R / 2 =$   $R(km) = 0.15 T_R (\mu s) \text{ or } \frac{C T_R}{2}$   $R(nmi)=0.081 T_R (\mu s)$  $If T_R = 1\mu s, R = 150 \text{ meters} = 164 \text{ Yards} = 492 \text{ ft.}$ 

1 Km=0.62137 statue mile = 0.53995 nautical miles 1 statue mile = 5280 ft = 1.60934 Km 1 Nautical mile = 6076.12 ft=1.852 Km
# **TARGET RANGE**

• Target range =

=

Measurement time  $(T_R) \times \text{Speed of light (C)}$ 

2

# **RELATION BETWEEN PRF, PRT & PRI**

- >PRF = Pulse Repetition frequency(HZ)
- PRT = Pulse Repetition Time (secs)
- >PRI = Pulse Repetition Interval (secs)

$$ightarrow PRF = \frac{1}{PRT} = \frac{1}{PRI}$$

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#### **MAXIMUM DETECTION RANGE**

PRT	PRF	MAXIMUM DETECTION RANGE
10 µs	100 KHZ	1.5 KMS
100 µs	10 KHZ	15 KMS
1000 µs	1 KHZ	150 KM

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#### **UNAMBIGUOUS RANGE**

>T<sub>R</sub> is the time elapsed between transmission pulse and Echo pulse.

But 
$$T_R = \frac{2 R}{C}$$
 where R= Range of target

T<sub>R</sub> increases with Range R and in extreme case Echo pulse merges with Transmitted Pulse

$$T_{R \max} = T_{P} \text{ and } R \text{ thus becomes } R_{\max}$$

$$T_{P} = Pulse \text{ Repetition Time}$$

$$T_{R \max} = T_{P} = \frac{2 \text{ Rmax}}{C} R_{\max} \text{ also known as}$$

$$Max R_{unambiguous} \qquad So R_{\max} = \frac{C TP}{2}$$

#### **UNAMBIGUOUS RANGE**

- When a pulse is transmitted, the Radar receiver listens for echoes until the next pulse is transmitted. This means that echoes must reach the Receiver within the pulse interval T<sub>P</sub>
- Unambiguous Maximum Range is the maximum range the radar is capable of determining without ambiguity .If the range of target is more than Unambiguous Max Range, multiple time around echoes occur and range computed is erroneous

# **RELATION BETWEEN UNAMB R<sub>MAX</sub> AND PRF**

≻Unamb 
$$R_{max} = \frac{C T_P}{2}$$
 (from earlier slide)

$$\succ$$
But PRF =  $\frac{1}{T_P}$  =  $\frac{C}{2 R_{max}}$ 

So Unamb 
$$R_{max} = \frac{C}{2 PRF}$$

➤The relation between PRF and Unamb R<sub>max</sub> is linear and shown in the graph.



Maximum Unambiguous Range Vs Pulse Repetition Frequency

#### Range Ambiguity – True Range



#### Tektronix<sup>.</sup>

#### Range Ambiguity – False Range



Target range  $R = c\Delta t_{perceived} / 2$ 

#### SECOND/MULTIPLE TIME AROUND ECHOES – RANGE AMBIGUITIES



# SECOND/MULTIPLE TIME AROUND ECHOES – RANGE AMBIGUITIES

➢ Display above gives the Range as 3 Kms (20 µs) whereas actual Range of target is 18 Kms. This is called Range Ambiguity.

➢ Maximum unambiguous range is the range beyond which target echo appears as second or multiple time around echo.

≻Unambiguous Range for this Radar is 15 Kms.

# SECOND/MULTIPLE TIME AROUND ECHOES – RANGE AMBIGUITIES

> VARIABLE PRT



#### **RELATIONS BETWEEN RADAR PARAMETERS**

1. R= 
$$\frac{C T_R}{2}$$

2. Unambiguous 
$$R_{max} = \frac{C T_p}{2}$$

3. Minimum Range 
$$R_{min} = \frac{C \tau}{2}$$

4. Range Resolution = 
$$\frac{1}{\tau}$$

5. Duty Cycle= 
$$\frac{\text{Pulse width}}{\text{Pulse repetetion time}} = \frac{\tau}{T_P}$$

#### **RELATIONS BETWEEN RADAR PARAMETERS**

6. 
$$f_P = \frac{1}{T_P}$$

7. Average Power 
$$P_{avg} = P_T \times \frac{\tau}{T_P}$$

- 8. Energy transmitted =  $P_T \times \tau$
- 9. Bandwidth =  $\frac{1}{\tau}$

#### **RADAR POWER PEAK AND AVERAGE POWER**

(Intub) Briefly discuss about the radar waveforms with respect to Peak Power, Average power, Duty cycle.



Peak power  $P_T = 1 \text{ MW}$ ; PRT = 1 milli sec so PRF = 1/PRT = 1/1x10<sup>-3</sup> =1000HZ Pulse width = 1 micro sec ;

#### **RADAR PEAK POWER AND AVERAGE POWER**

• Average Power  $P_{avg} = P_T \times \frac{\tau}{T_p} = P_T \tau f_P$ 

• 
$$P_{avg} = 1 \times 10^6 \times \frac{1 \times 10^{-6}}{1 \times 10^{-3}} = 1000 \text{ W} = 1 \text{ KW}$$

• Duty cycle = 
$$\frac{\tau}{T_p} = \frac{1 \times 10^{-6}}{1 \times 10^{-3}} = 0.001$$

• Energy of pulse =  $P_T x \tau$  = 1x 10<sup>6</sup> x 1x 10<sup>-6</sup> = 1 joule

#### **RADAR WAVE FORMS**

(Intuh) Discuss briefly about the radar waveforms
1.CW Radar:



- CW Radar has monotonic unmodulated continuous wave forms.
- Well suited for extracting radial velocity of target using Doppler principle.
- Can not give range of target

# **RADAR WAVE FORMS(contd)**

# 2. Modulated CW Radar (Sinsoidal Modulation)



- Gives the radial velocity and range of target
- Other modulations are Triangular ,sawtooth etc.,

# **RADAR WAVE FORMS(contd)**

#### 3. Pulse Radar (Pulse Modulated CW Radar)



- Extensively used for Range Determination
- Modified Pulse Radar in the name of Pulse Doppler
- radar and MTI Radar is used for obtaining radial velocity

#### **RADAR WAVE FORMS(contd)**

• Pulse Radar (Envelop of Tx and Rx pulses)



#### **RADAR PROBLEMS**

Intuble 1 Calculate the range of the target , if the time taken by the signal to travel and return is 100 microsecs.

Given TR = 100 microsec = 100x 10-6 secs
 To find R = ?

• 
$$R = \frac{C T_R}{2}$$
 (from the formula)

• 
$$R = \frac{3 \times 10^8 \times 100 \times 10^{-6}}{2} = 15000 \text{ mts} = 15 \text{ Kms}$$

#### **RADAR PROBLEMS(contd)**

2 What should be the pulse repetition frequency and duty cycle of radar in order to achieve a maximum unambiguous range of 60 nmi with a pulse width of 1.5 μs ?
Given : 1. Max unambiguous range = 60 nmi = 60 x 1.852 x 10<sup>3</sup> meters

(1nmile = 1.852Km)

•2. Pulse width =  $\tau$  =1.5 µs= 1.5 x 10<sup>-6</sup> sec

•Find fp= Pulse repetition frequency  $fp = \frac{C}{2R_{max}} = \frac{3 \times 10^8}{2 \times 60 \times 1.852 \times 103} = 1349.89 \text{ Hz}$   $Tp = \frac{1}{fp} = \frac{1}{1349.89} \text{ sec}$ 

• Duty cycle =  $\frac{\tau}{Tp}$  = 1.5 x 10<sup>-6</sup> × 1349.89 = 0.0020248

### **RADAR PROBLEMS(contd)**

3. The unambiguous range of radar is 200 Kms.It has a bandwidth of 1.0 MHz. find i) Pulse repetition frequency ii) Pulse width

- Given: Rmax = 200 km and Band width = 1.0 MHz Find fp and  $\tau$
- Answer: Pulse repetition frequency fp =  $\frac{C}{2 R_{max}}$  =

• fp = 
$$\frac{3 \times 10^6}{2 \times 200 \times 10^3}$$
 = 750 Hz  
• Pulse width  $\tau = \frac{1}{\text{Band width}} = \frac{1}{1 \times 10^6} = 1 \,\mu\text{sec}$ 

# **TO BE CONTINUED IN 1C**

# **RADAR SYSTEMS** (Jntuh) EC812PE: RADAR SYSTEMS (PE - V) UNIT - 1C**B.TECH IV YEAR II SEMESTER** BY **Prof.G.KUMARASWAMY RAO** (Former Director DLRL Ministry of Defence) BIET

# Acknowledgements

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# SIMPLE FORM OF RADAR RANGE EQUATION

#### SIMPLE FORM OF RADAR RANGE EQUATION



### SIMPLE FORM OF RADAR RANGE EQUATION

- Radar Equation is relation between
- (1) Transmitter Power
- (2) Receiver Power
- (3) Antenna Characteristics
- (4) Target Cross section
- (5)Frequency of Transmission
- (6)Environmental Noise
- Radar Equation is most useful for (i)Design (ii)Implementation (iii)Testing of Radar System

# **ISOTROPIC ANTENNA (CONCEPT)**

An isotropic antenna (also known as an <u>omnidirectional</u> <u>antenna</u>) emits the signal uniformly in all directions. In other words, at distance '*R*' from the antenna, in any direction, the transmitted signal power is the same. Although building a truly omnidirectional antenna is not feasible, this ideal antenna is frequently used to simplify range estimation analysis as well as provide a reference point in comparing different types of antennas.

#### **Radar Range Equation (Contd....)**



Isotropic (Omni) Antenna radiates Power in all directions uniformly

#### **Radar Range Equation**



# **Omni Antenna Radiation Pattern**



# **Radar Range Equation (contd..)**

 $\mathbf{P}_{T}$  = Transmitted Power (watts)

Ξ

- Antenna assumed Isotropic ie., radiates power in all directions
- Power Density at a distance 'R' from Radar =Power density on the surface of the sphere with radius 'R'
  PT
  - Surface Area of Sphere of Radius 'R'  $\frac{P_T}{4 \pi R^2}$

#### **Radar Range Equation (continued)**



# Radar Range Equation (Contd....)

- Radar Antennas are Directional
- $\succ$  G<sub>T</sub> = Gain of Antenna =

Power Density in Directive Antenna

Power Density in Isotropic Antenna



Power Density at Range 'R' from Directive Antenna

 $= \frac{P_T \times G_T}{4 \pi R^2}$
#### Definition of Radar Cross Section (RCS or $\sigma$ )



Radar Cross Section (RCS or σ) is a measure of the energy that a radar target intercepts and scatters back toward the radar

Power of reflected signal at target

$$\frac{\mathsf{P}_{t}\,\mathsf{G}_{t}}{4\,\pi\,\mathsf{R}^{2}}$$

σ = radar cross section units (meters)<sup>2</sup>

#### Radar Range Equation (Contd....)



Echo Power density at Receiver at distance R from target

$$\frac{P_T G_T}{4 \pi R^2} \times \frac{1 \times \sigma}{4 \pi R^2}$$

#### Radar Range Equation (Contd....)

The received power = the power density at the radar times the area of the receiving antenna

Power of reflected signal from target and received by radar  $P_r = \frac{P_t G_t}{4 \pi R^2} \frac{\sigma A_e}{4 \pi R^2} P_r = power received$   $A_e = effective area of receiving antenna$ 

Where A<sub>e</sub>=Aperture area of receiving antenna
Power received at the output of Antenna = P<sub>R</sub>  $\frac{P_T G_T \sigma}{[4 \pi R^2]^2} \times A_e$ If Dense (D) increases D, decreased with it is an

If Range 'R' increases, P<sub>R</sub> decreases until it is equal to S<sub>min</sub>=Minimum Detectable signal by the Receiver and R= R<sub>max</sub>

#### **Radar Range Equation (Contd....)**

$$\succ S_{\min} = \frac{P_T G_T \sigma}{[4 \pi R_{\max}^2]^2} x A_e$$

$$\succ R_{\max} = \frac{\left[\frac{P_T G_T \sigma A_e}{[4 \pi]^2 x S_{\min}}\right]^{\frac{1}{4}}$$

#### The above is called Radar Range Equation-----(A)

#### **ALTERNATE FORMS OF RADAR RANGE EQUATION**

$$R_{\max} = \begin{bmatrix} \frac{P_T \ G_T \ \sigma \ A_e}{[4 \ \pi \ ]^2 \ S_{\min}} \end{bmatrix}^{\frac{1}{4}} \quad (A)$$
• From Antenna Theory
$$G_R = \frac{4 \ \pi \ A_e}{\lambda^2}$$

Where  $G_R$  = Receiving Antenna Gain

$$\lambda$$
 =Wavelength ( $\lambda = \frac{C}{f}$ )

So 
$$A_e = \frac{G_R \lambda^2}{4 \pi}$$

Alternate Forms Of Radar Range Equation (Contd....)

Substituting 
$$A_e$$
 in Equation (A)  
 $R_{max} = \left[ \frac{P_T \ G_T \ \sigma \ G_R \ \lambda^2}{[4 \ \pi \ ]^3 \ S_{min}} \right]^{\frac{1}{4}}$ 

➢ If same antenna is used for transmission and reception.G<sub>T</sub>=G<sub>R</sub>=G

#### **Alternate Forms of Radar Range Equation (Contd..)**

Since 
$$G = \frac{4 \pi A_e}{\lambda^2}$$

Substituting this in Equation B. We get

$$P_{\text{max}} = \left[ \frac{P_{\text{T}} \ \text{G}^{2} \ \sigma \ \lambda^{2}}{[4 \ \pi \ ]^{3} \ \text{S}_{\text{min}}} \right]^{\frac{1}{4}} - \dots (B)$$

$$P_{\text{max}} = \left[ \frac{P_{\text{T}} \ A^{2} \ \sigma}{4 \ \pi \ \lambda^{2} \ \text{S}_{\text{min}}} \right]^{1/4} - \dots (C)$$

#### **THREE FORMS OF RADAR EQUATION**

$$R_{\max} = \left[\frac{P_{T} \ G_{T} \ \sigma \ A_{e}}{[4 \ \pi \ ]^{2} \ S_{\min}}\right]^{\frac{1}{4}} \qquad ----- A$$

$$R_{\max} = \left[\frac{P_{T} \ G^{2} \ \lambda^{2} \ \sigma}{[4 \ \pi \ ]^{3} \ S_{\min}}\right]^{\frac{1}{4}} \qquad ----- B$$

$$R_{\max} = \left[\frac{P_{T} \ A^{2} \ \sigma}{4 \ \pi \ \lambda^{2} \ S_{\min}}\right]^{1/4} \qquad ----- C$$

## Relation between R<sub>max</sub> and P<sub>T</sub> when other parameters are held constant

$$R_{\text{max}} = \left[\frac{P_{\text{T}} \ \text{G}^2 \ \lambda^2 \ \sigma}{[4 \ \pi \ ]^3 \ \text{S}_{\text{min}}}\right]^{\frac{1}{4}}$$

 $\blacktriangleright$  When all parameters like G,  $\lambda$  ,  $\sigma$  ,  $S_{min}$  are held constant

$$> R_{max} = K P_T^{1/4}$$

Range Vs  $P_{T}$ 

Range	P <sub>T</sub>
2 Times	16 Times
3 Times	81 Times
Half	1/16 Times (1/2) <sup>4</sup>

# RADAR RANGE EQUATION (ANSWER TO JTUH QUESTION)

- (Jntuh) (Jntuh) (Jntuh)
- Derive the radar range equation/ Derive the basic radar equation/Derive the maximum range for a radar system from first principles/Obtain the basic radar equation in terms of minimum detectable power, gains of transmitting and receiving antennas etc.

- Radar Equation is relation between
- (1) Transmitter Power
- (2) Receiver Power
- (3) Antenna Characteristics
- (4) Target Cross section
- (5)Frequency of Transmission
- (6)Environmental Noise
- Radar Equation is most useful for (i)Design (ii)Implementation (iii)Testing of Radar System

- P<sub>t</sub> = Transmitted power of the radar
- Initially assume the antenna is isotropic. The isotropic antenna transmits power uniformly in all directions as shown in figure





- Let the target be at a distance of R from the antenna on an imaginary sphere of radius R
- Power density at any point on the sphere of radius R =  $\frac{P_t}{4 \pi R^2}$
- Since instead of isotropic antenna Directional antenna is used in practice

 Power Density of directional antenna = Power Density of Isotropic antenna × Transmitting Gain

 $= \frac{P_t}{4 \pi R^2} \times G_t \text{ where } G_t \text{ is the gain of transmitting antenna}$ 

- Let us assume the radar cross-section of the target is σ (sigma). The σ is defined as the amount of transmitted power intercepted by the target and reradiated back in the direction of the radar antenna
- So the power reradiated from target =  $\frac{P_t}{4\pi R^2} \times G_t \times \sigma$
- This reflected signal acts a microwave source and spread power in all directions like a Omni antenna

- Power density of reradiated signal at the radar antenna =  $\frac{\frac{P_t}{4 \pi R^2} \times G_t \times \sigma}{4 \pi R^2} = \frac{P_t G_t}{4 \pi R^2} \frac{\sigma}{4 \pi R^2}$
- Let the antenna has an Effective aperture area of  $A_e$ . A portion of the reradiated power is captured by the radar antenna.
- The received power Pr by the radar antenna  $= \frac{P_t G_t}{4 \pi R^2} \frac{\sigma}{4 \pi R^2} A_e = \frac{P_t G_t A_e \sigma}{(4 \pi R^2)^2}$ •  $P = \frac{P_t G_t A_e \sigma}{P_t G_t A_e \sigma}$

• 
$$P_{\gamma} = \frac{t - t - c}{(4 \pi R^2)^2}$$

$$\Pr = \frac{\Pr G_t A_e \sigma}{(4 \pi R^2)^2)}$$

• Let Rmax is the maximum range beyond which the Pr becomes small so that radar receiver stops detecting the target. At this Rmax Pr is denoted as Smin. So Pr = Smin

• Smin = 
$$\frac{P_t G_t A_e \sigma}{(4 \pi R_{max}^2)^2}$$
  
•  $R_{max} = \left[\frac{P_t G_t A_e \sigma}{(4 \pi)^2 S_{min}}\right]^{\frac{1}{4}}$  This is called the Radar equation

- . R<sub>max</sub> =  $\left[\frac{P_t G_t A_e \sigma}{(4 \pi)^2 S_{\min}}\right]^{\frac{1}{4}}$
- The above is called the basic Radar Range Equation or the first Radar Range Equation
- Second Form of Radar Range equation:
- From Micro wave theory we know that  $G_{r} = \begin{bmatrix} \frac{4 \pi A_{e}}{\lambda^{2}} \end{bmatrix}$ Substituting this value in the basic radar equation. But  $G_{t} = G_{r} = G$  since single antenna is used •  $R_{max} = \left[\frac{P_{t} \frac{4 \pi A_{e}}{\lambda^{2}} A_{e} \sigma}{(4 \pi)^{2} S_{min}}\right]^{\frac{1}{4}} = \left[\frac{P_{t} A_{e}^{2} \sigma}{4 \pi \lambda^{2} S_{min}}\right]^{\frac{1}{4}}$ This is called the second form Radar equation

- Third Form of Radar Range equation:
- Substituting  $\boldsymbol{A}_e~$  in the above equation

• 
$$R_{max} = \left[\frac{P_t G^2 \lambda^2 \sigma}{(4 \pi)^3 S_{min}}\right]^{\frac{1}{4}}$$
 this is called the Third form of Radar range equation

• Intuh) Three forms of Radar Range Equation

• 
$$R_{max} = \left[\frac{P_t G_t A_e \sigma}{(4 \pi)^2 S_{min}}\right]^{\frac{1}{4}}$$
 First Form  
•  $R_{max} = \left[\frac{P_t A_e^2 \sigma}{4 \pi \lambda^2 S_{min}}\right]^{\frac{1}{4}}$ Second Form  
•  $R_{max} = \left[\frac{P_t G^2 \lambda^2 \sigma}{(4 \pi)^3 S_{min}}\right]^{\frac{1}{4}}$ Third form

(Jntuh) .Derive the Radar Range equation

- Let us assume a Transmitter which gives out a peak power P<sub>T</sub>
- For analysis sake, let it be connected to a Omni (isotropic antenna). Omni antenna transmits RF energy in all directions
- Power density on any point on an imaginary sphere of radius R is  $\frac{P_T}{4 \pi R^2}$
- In practical field , a directional antenna is used in place of omni antenna to avoid wastage of power. Let its gain =  $G_T$

- The Power density on the sphere with radius R with directional antenna =  $\frac{P_T}{4 \pi R^2} G_T$
- Assume there is a target with a cross-section  $\sigma$  on the outer surface of the sphere
- But Power = Power density x Area
- So the power reflected by the target is  $\frac{P_T}{4\,\pi\,R^2}\;G_T\;\sigma$
- The reflected power acts as a microwave source and radiates RF power in all directions (like an Omni antenna)

• The power density at the receiving antenna which is on a sphere of radius R =  $\left[\frac{P_T}{4 \pi R^2} G_T \sigma\right] \frac{1}{4 \pi R^2}$ 

• 
$$\mathsf{R} = \frac{\mathsf{P}_{\mathrm{T}} \,\mathsf{G}_{\mathrm{T}} \,\sigma}{(4 \,\pi \,\mathsf{R}^2)^2}$$

- If the aperture area of receiving antenna = Ae
- Then the power received at the output of receiving antenna  $\mathsf{P}_\mathsf{R}$

• 
$$P_{R} = \left[\frac{P_{T} G_{T} \sigma}{(4 \pi R^{2})^{2}}\right] A_{e}$$

- P<sub>R</sub> denotes the receiving power and denotes the sensitivity of receiver
- $P_R$  keeps decreasing when R is increasing. At some value of R=  $R_{max}$ ,  $P_R = S_{min}$  where  $S_{min}$  is the minimum receiver power, less than  $S_{min}$  radar does not function

• 
$$S_{min} = \left[\frac{P_T G_T \sigma A_e}{(4 \pi R_{max}^2)^2}\right] = \left[\frac{P_T G_T \sigma A_e}{(4 \pi)^2 (R_{max})^4}\right]$$
  
•  $(R_{max})^4 = \left[\frac{P_T G_T \sigma A_e}{(4 \pi)^2 S_{min}}\right]$ 

• 
$$R_{\max} = \left[\frac{P_T G_T \sigma A_e}{(4 \pi)^2 S_{\min}}\right]^{\frac{1}{4}} ----EQ-A$$

- This is called Radar Range equation
- From Microwave theory  $G_R = \frac{4 \pi A_e}{\lambda^2}$  where  $G_R$  is the gain of receiving antenna, Same antenna is used for transmission and reception. So  $G_R = G_T = G$

• Substituting 
$$A_e = \frac{G \lambda^2}{4 \pi}$$
 in EQ- A, above we get

$$R_{max} = \left[\frac{P_T G^2 \sigma \lambda^2}{(4 \pi)^3 S_{min}}\right]^{\frac{1}{4}} EQ -B$$

• Substituting G= 
$$\frac{4 \pi A_e}{\lambda^2}$$
 in EQ-B we get  

$$R_{max} = \left[ \frac{P_T \left(\frac{4 \pi A_e}{\lambda^2}\right)^2 \sigma \ \lambda^2}{(4 \pi)^3 S_{min}} \right]^{\frac{1}{4}}$$

$$R_{max} = \left[ \frac{P_T A_e^2 \sigma}{(4 \pi) \lambda^2 S_{min}} \right]^{\frac{1}{4}} EQ-C$$

- Intuh) A pulsed radar operating at 10 Ghz. has an antenna with a gain of 28 dB and a transmitter power of 2 Kw (pulse power). If it is designed to detect a target with a cross section of 12 sq.m. and the minimum detectable signal is Pmin = −90 dBm. What is the maximum rangeof the radar?
- Frequency = 10 Ghz=  $10 \times 10^9$  Hz
- Antenna gain = 28 dB (antilog of  $\frac{28}{20}$  = 25.12)
- Transmitted Power =  $2 \text{ KW} = 2 \times 10^3 \text{ watt}$
- Target cross section = 12 sq.m

• Minimum detectable signal =  $S_{min} = -90 \text{ dBm} =$ -90 -30 = - 120 dBW = Antilog (- 120/10) = 10<sup>-12</sup> W

• 
$$R_{max} = \left[\frac{P_T G^2 \sigma \lambda^2}{(4 \pi)^3 S_{min}}\right]^{\frac{1}{4}}$$
  
•  $\lambda = \frac{C}{f} = \frac{3 \times 10^8}{10 \times 10^9} = 0.03 \text{ m}$   
•  $R_{max} = \left[\frac{2 \times 10^3 \times 25.12 \times 25.12 \times 0.03 \times 0.03 \times 12}{(4 \times \pi)^3 \times 10^{-12}}\right]^{\frac{1}{4}}$ 

•  $R_{max} = 1619 \text{ mt}$ 

- Intuh) Problem No.2 If the Radar is designed for operation at 10 GHz with an antenna diameter is 2m. Calculate the peak pulse power required to have a maximum range of 1000Km with a target of cross section area of 20 m<sup>2</sup>. assume minimum detectable noise power is 36 is 36 x 10<sup>-15</sup> W
- Given quantities: frequency = 10 Ghz Antenna diameter = 2 m Maximum range of radar =  $R_{max} = 1000$ Km =  $10^6$ m Cross sectional area = 20 m Minimum detectable noise power=  $S_{min} = 36 \times 10^{-15}$  W

• Solution:

Aperture area of antenna =  $\frac{\pi D^2}{4} = \frac{\pi 2^2}{4} = 3.14$  sq.m • Wave length  $\lambda = \frac{c}{f} = \frac{3 \times 10^8}{10 \times 10^9} = 0.03 \text{m}$ •  $R_{max} = \left| \frac{P_T A_e^2 \sigma}{(4 \pi \lambda^2 S_{min})} \right|^{\frac{1}{4}}$  $P_{\rm T} = \frac{4 \pi \lambda^2 S_{\rm min} R_{\rm max}^4}{A_{\rm o}^2 \sigma}$  $P_{\rm T} = \frac{4 \times 3.14 \times 0.03 \times 0.03 \times 36 \times 10^{-15} \times (1000 \times 10^3)^4}{3.14 \times 3.14 \times 20}$  $P_{T}$  = 2063694.268 W = 2.064 MW

## BLOCK DIAGRAM OF PULSE RADAR (ANSWER TO JNTUH QUESTION)

## **BLOCK DIAGRAM OF PULSE RADAR (JNTUH QUESTION)**

(Jntuh) (Jntuh) (Jntuh)

- Describe the working principle of Pulsed Radar System or
- 2. With a block diagram explain the operation of Pulse Radar

#### or

• 3. Draw the block diagram of a Pulsed Radar and explain its operation

### **RADAR SYSTEM BLOCK DIAGRAM**

 Radar shown in the block diagram is called mono-static Radar since same antenna is used for transmission and reception.



**BLOCK DIAGRAM OF RADAR SYSTEM** 

**Block Diagram of Pulse Radar (Answer to Jntuh Question)** 

• BLOCK DIAGRAM OF PULSE RADAR.



### **Block Diagram of Pulse Radar (Answer to Jntuh Question)**

- 1. TIMER: This generates a series of narrow timing trigger pulses at pulse repetition frequency of radar. This is also called trigger generator or synchronizer. This is a small unit compared to the Modulator.
- 2. MODULATOR: The narrow trigger pulses when given to the modulator, generates the fixed duration radar pulses whose pulse width ranges from sub microsecs to a few microsecs. The frequency of these pulses is the Pulse repetition frequency of the radar.



#### **Block Diagram of Pulse Radar (Answer to Jntuh Question)**

#### • 3. TRANSMITTER:

A typical radar may detect aircraft at ranges from 50 to 500 kms. It employs a peak power of the order of 1 to 10 Mega watts. The transmitter generates modulated RF pulses. The modulated RF energy travels along the transmission line to the antenna


## 3. TRANSMITTER(contd)

There are two types of Transmitters

(i) Power Oscillator Ex:Magnetron-1 M Watt or more.

Pulse Modulator switches power on or off

(ii) Power Amplifier: Ex: Klystron, TWT Amplifies LowPower signal

 4. DUPLEXER: Single antenna is used for both transmission and reception. The Duplexer unit connects the Transmitter to the antenna while transmitting. It disconnects the Receiver from the antenna during transmission. The Receiver also is disconnected from the Transmitter to avoid damage to the sensitive receiver since the transmitting power is very high.

#### • 4. DUPLEXER: (contd)

While receiving target echoes from target, the Duplexer unit connects the Receiver to the antenna. It disconnects the Transmitter from the antenna during this period. This is done in order to avoid even a small portion of echo power gets connected to Transmitter and getting wasted. Since the switching speed is in nano secs, Gas Discharge tube is used.

- 4 Duplexer consists of TR and ATR switch. 4(a) TR (Transmit and Receive Switch): This is a fastacting switch which disconnects Receiver during transmission. If the Receiver is not disconnected, since the transmitter power is very high, the Receiver may be damaged. Once the pulsed RF signal has stopped the TR switch reconnects the Receiver to the antenna. The target echo power received enters the Receiver
- 4(b) ATR (Anti Transmit and Receive Switch): ATR switch do not act during transmission. During reception it switches and disconnects transmitter from antenna. If ATR is absent, a portion of the received power would go to transmitter rather than all the power going to the Receiver

(i)Antenna converts the Electrical signal to Electro magnetic signal and radiates it into space.

(ii)Same antenna is used for transmission and reception in a Pulse Radar.

(iii)Antenna is mounted on a pedestal and servo controlled to steer it in the direction of the target.(iv)Normally parabolic Antenna is used for radar applications

## 6. LOW NOISE RF AMPLIFIER: (LNA)

- (i)This is a RF Amplifier such as parametric amplifier or Low Noise transistor amplifier.
- (ii)LNA is used immediately after the antenna since the power of the echoes are very low
- (iii) Gain of LNA reduces the Noise Figures of the succeeding devices by dividing the N.F. of the device by the Gain of the LNA.

## 7.MIXER & LOCAL OSCILLATOR

- Receiver uses super heterodyne principle
- (i) Converts R.F. Signal to I.F. (Intermediate Frequency)
- (ii) IF is usually at 30 MHZ or 60 MHZ. With a bandwidth of 1 to 2 MHz. It is easier to design and build High gain amplifiers and filters at IF frequencies. Widespread availability of components at these frequencies is also one of the reasons for Superheterodyning
- (iii) L.O. frequency is  $f_L = f_{RF} \mp 30$  MHZ,
- where  $f_{RF} = RF$  frequency and  $f_L = LO$  frequency

# Block Diagram of Pulse Radar (Answer to Jntuh question)7 MIXER & LOCAL OSCILLATOR (contd)



## 8. IF AMPLIFIER & MATCHED FILTER

- (i)The signal level of Echo, is very low. It is amplified to an appropriate level by the IF Amplifier.
- (ii)The I.F. centre frequency is 30 MHZ with a band width of 1 MHZ (depending on Pulse width)
- (iii)The matched filter frequency response is such that it maximizes the peak signal to mean noise power ratio at output.
- (iv)Usually the IF Amplifier and matched filter are designed into a single subsystem.

## 9. 2<sup>ND</sup> DETECTOR

(i)2<sup>nd</sup> Detector removes the IF modulation.

(ii)Output of the 2<sup>nd</sup> Detector is the Video Pulse.

(iii)2<sup>nd</sup> Detector is the high frequency diode.

(iv)It is called as 2<sup>nd</sup> Detector since it is the second diode used in the chain. The first diode is used in the mixer.

#### **10.VIDEO AMPLIFIER**

The low signal level of Video Pulse is amplified such that the voltage level is high enough to drive the CRT (Cathode Ray Tube). CRT is used as the Display.



i)The Display is generally a CRT (Cathode Ray Tube)
(a) 'A' scope (b) PPI(Plan position indicator) etc.
(ii)'A' scope provides Range and Echo power.
(iii)PPI measures Range and bearing (azimuth angle)
(iv)In addition there are other displays like 'B' scope,
' D ' scope etc.

## **PRACTICAL RADAR DISPLAY**



## **RANGE & DIRECTION IN A PULSE RADAR**

Intuh Discuss how the Direction and range of an object is determined using Pulse Radar



## **RANGE & DIRECTION IN A PULSE RADAR**

- PPI –SCOPE: The output from the Video Amplifier Of Pulse Radar is displayed using PPI (Plan Position Indicator) scope. PPI maps the position of target in azimuth and range. North is taken as the reference direction. PPI scope is an intensity modulated circular display. The range and angle is displayed in polar coordinates.
- A SCOPE: This display also plots the range and angle of the echo signal. It is connected to the output of Video amplifier. X axis gives the range and Y axis displays the amplitude of echo signal

## **RADAR FREQUENCIES**

## **RADAR FREQUENCIES**

- Untuh) Discuss about Radar Frequencies
- RF spectrum is very scarce and as such Radars are allotted only a certain frequency bands for its operation by International Telecom Union ITU
- During 2<sup>nd</sup> world war to keep the secrecy, certain code words were used. They are L,S,C,X, Ku,K,Ka etc. The same designations are continued.
- Lema Band(L)1GHZ-2GHZ, Sierra band(S) 2GHZ- 4GHZ, Charlie Band (C) 4GHZ-8GHZ, Xera Band (X) 8GHZ-12GHZ
- ITU(International Telecommunication Union) allocates a portion of these bands for Radar use.

## **ELECTROMAGNETIC SPECTRUM (contd..)**

#### Atmospheric attenuation vs frequency





IEEE Standard Radar Bands (Typical Use)			
HF	3 – 30 MHz		
VHF	30 MHz–300 MHz 🕇	Search	
UHF	300 MHz–1 GHz	Radars	
L-Band	1 GHz–2 GHz 🔸	1	
S-Band	2 GHz–4 GHz	Search & Track Radars	
C-Band	4 GHz–8 GHz 🕇		
X-Band	8 GHz–12 GHz	Fire Control & ▲ Imaging Radars	
Ku-Band	12 GHz–18 GHz 🔸		
K-Band	18 GHz–27 GHz	Missile	
Ka-Band	27 GHz-40 GHz	Seekers	
W-Band	40 GHz – 100+ GHz	+	



## **STANDARD FREQUENCY BANDS**

Band designation	Nominal frequency range	Specific radiolocation (radar) bands based on ITU assignments for region 2
HF	3-30 MHz	
VHF	30-300 MHz	138-144 MHz
		216-225
UHF	300-1000 MHz	420-450 MHz
	0	890-942
L	1000-2000 MHz	1215-1400 MHz
S	2000-4000 MHz	2300-2500 MHz
		2700-3700
C	4000-8000 MHz	5250-5925 MHz
X	8000-12,000 MHz	8500-10,680 MHz
K.	12.0-18 GHz	13.4-14.0 GHz
200-0 <b>-0</b>		15.7-17.7
K	18-27 GHz	24.05-24.25 GHz
K.	27-40 GHz	33.4-36.0 GHz
mm	40-300 GHz	

## **CAPABILITIES OF RADAR**

## **CAPABILITIES OF RADAR**

- 1. Detect, locate & identify aircraft for Air Traffic Control(ATC).
- 2. Detect, locate & classify aircraft(Friend or Foe) for military purpose.
- 3. Locate ships and land features for ships collision avoidance.
- 4. Navigate ships and aircrafts even in bad weather (rain, snow fog, storm, cyclone etc). or in night.
- 5. Measures height of flying aircraft, helicopter
- 6. Give early warning of intruding enemy aircraft or missile.

### **CAPABILITIES OF RADAR( contd....)**

- 7. Provide accurate three dimensional co-ordinates of enemy aircraft for gun control or missile guidance.
- 8. As a part of Geographical survey, maps land and sea areas from space.
- 9. Remote sensing of agriculture crops and their pattern using special signal processing techniques.
- 10.Detect mines and foreign objects inside the grounds.
- 11.Measure speeding motor vehicle's, speed for use by Law enforcing authorities.
- 12.Used for Space vehicle docking and landing on moon, Mars etc.

- (Intuh) Explain about applications of Radar
- Radar has wide range of applications. They are used on ground, in air, in sea and in space. They can be broadly divided into i) Civilian use and ii) Military use
- CIVILIAN USE:
- 1. AIR TRAFFIC CONTROL (ATC):

Radars are without exception used in the Airports for controlling the Aircraft traffic. A high resolution radar is used to monitor the aircraft and guide the pilots to safely land on the runways and take off. In bad weather and poor visibility conditions in association with GCA (Gound Control Approach) radar is used to guide the aircraft safely to land.

## •2. AIRCRAFT NAVIGATION:

a) All modern aircrafts are fitted with 'Weather Avoidance Radars'. These radars give warning information about the outline regions of precipitation of snow or storms to the pilot lying ahead of aircrafts path. Some radars are used for terrain avoidance and terrain following. Ground mapping radars can be mounted on aircrafts for terrain mapping purposes. b) Radar is mounted on Helicopters and used as altimeter to indicate the height of Helicopter from the ground

• 3. MARITIME RADARS FOR SHIPS SAFETY AND NAVIGATION:

•Large portion of our merchandise between nations is transported through sea. Because of poor visibility in sea due to haze, smoke, rain, storm, cyclone etc. possibility of collision of Ships is high. Using radars mounted on ships, collision of ships can be avoided in the middle of sea.

•Radars guide ships in seaports safely.

### • 4. SPACE:

Radar is used for rendezvous and docking of space vehicles and landing of space vehicles on Celestial objects like moon, mars etc.

Ground based radars are used for tracking of satellites

## **5.REMOTE SENSING:**

Radar is used as a remote sensor of the weather. The earth resources which are to be probed by the radar are i) Measurement and mapping of sea conditions ii)water resources iii) ice cover iv) agriculture and forestry conditions v) environmental pollution vi) geological formations

## 6. LAW ENFORCING AGENCIES:

Radars are used by Police personnel to measure and restrict the speed of automobile vehicles to avoid fatal accidents.

## 7.MILITARY USE:

- Radars are widely used in military applications.
- (i)Early warning of intruding enemy aircrafts & missile
- (ii)Tracking hostile targets and providing location
  - information to Air Defense systems consisting of Tracking Radars controlling guns and missiles.
- (iii)Battle field surveillance
- (iv)Information Friend or Foe IFF
- (v)Navigation of ships, aircrafts, helicopter etc.

## World War 2 Air Defense System



Courtesy of US Army

#### **Surveillance and Fire Control Radars**















#### **Airborne Radars**



#### **Civil Radars**



#### More Civil Radars
















(Intuh) List out major applications of Radar in military
 1. GROUND PENETRATING RADAR :

These type of Radars are useful for finding out Land mines buried a few centimeters beneath the ground surface. The radars can detonate these mines and make movement of persons or vehicles safe. If the moisture content of soil is not very high, radar signals can penetrate into the ground.

•2. AREA SURVEILLANCE OR GROUND SURVEILLANCE: These radars are kept on tripods and keep watching in a particular direction over an area. They give alert when there is an activity in that area like an intruder approaching, crawling, running etc. they are called BFSR (Battle field surveillance Radar)

#### •3. AIR SURVEILLANCE RADARS:

For detecting enemy aircraft and directing defensive measures against them monitoring of airspace is required. For better and maximum coverage these radars are located on airborne platforms for detecting low height flying hostile aircrafts. These are called AWACS (Airborne Warning and Control System). OTH (Over The Horizon) radars exploit certain ground features and can detect low flying aircrafts at thousands of kilometers away

#### 4. TARGET TRACKING RADAR:

Target tracking is associated with Gun control weapon and Missile weapon system. They track the incoming hostile aircraft in azimuth and elevation very accurately using the principle of Mono-pulse. The location of hostile aircraft in three (azimuth, elevation and range) coordinates will be provided to the weapon system like the Gun control weapon or to the guided missile so that the hostile target is shot down.

In case of multiple target tracking radar beam is quickly switched from one position to other and thus multiple target tracking is accomplished, These Radars are called Phased array radars PROF.G.KUMAR 220

# **CONTINUED IN RADAR 1D**

# **RADAR SYSTEMS** (EC 812 PE) (ELECTIVE V) UNIT - 1D**B.TECH IV YEAR II SEMESTER** BY **Prof.G.KUMARASWAMY RAO** (Former Director DLRL Ministry of Defence) BIET

# Acknowledgements

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PROF.G.KUMARASWAMY RAO BIET

• (Intub) Explain the prediction of range performance OR

Discuss in detail the choice of various parameters that are affecting the radar range

#### OR

Briefly discuss about the prediction of range performance

$$\bigstar R_{\text{max}} = \left[ \frac{P_T \ G_T \ \sigma \ A_e}{[4 \ \pi \ ]^2 \ S_{\text{min}}} \right]^{\frac{1}{4}}$$

- ✤ P<sub>T</sub> = Transmitted Power (watts)
- $G_T$  = Transmitting Antenna Gain (number)
- ✤  $A_e$  = Receiving Antenna Effective aperture mt<sup>2</sup>
- $\bullet \sigma$  = Radar cross-section mt<sup>2</sup>
- ✤ S<sub>min</sub> = Minimum Detectable Signal (Watts)
- Except for σ (RCS) all the other above quantities are design parameters . σ is random with respect to angle and given as a statistical quantity

 Radar Cross section σ varies randomly with a slight change in the angle of incident of RF energy



# **PREDICTION OF RANGE PERFORMANCE(CONTD..)**

- If long Range (Rmax) is desired the following are required
- $\succ$  i) P<sub>T</sub> Transmitted Power must be high
- ➢ ii) G<sub>T</sub> should be high. For this Transmitted Power must be concentrated into a narrow beam
- iii) A<sub>e</sub> must be high. Large aperture antenna is necessary
- iv) S<sub>min</sub> must be low. Receiver must be sensitive to weak signals

#### PREDICTION OF RANGE PERFORMANCE(CONTD..)

- Practical Range obtained using the above Range equation is often less because we have not considered the following aspects
- i) Various losses because of Electronic equipment used in operational field
- ii)  $\sigma$  are statistical in nature .  $\sigma$  change with even a small change in angle
- iii) Meteorological conditions during propagation
- iv) Performance of radar operator
   Because of the above R<sub>max</sub> cannot be given by a single number

#### **PREDICTION OF RANGE PERFORMANCE(CONTD..)**

- Radar range can only be predicted with a certain probability for a practical target
- The Radar will detect a given target at a particular range by including the term probability in its radar equation

# MINIMUM DETECTABLE SIGNAL, RECEIVER NOISE AND SNR

# MINIMUM DETECTABLE SIGNAL

# MINIMUM DETECTABLE SIGNAL

What is meant by minimum detectable signal in radar

S<sub>min</sub> – Signal detectable by a Receiver (Rx) is limited by Noise energy that is present in the frequency spectrum of signal energy

#### NOISE



# **MINIMUM DETECTABLE SIGNAL**

# Minimum Detectable signal (S<sub>min</sub>):

Minimum Detectable signal is the weakest signal the Receiver can detect

Presence or absence of a target is determined by

- i)  $S_{min}$
- ii) threshold criterion

iii) human operator

#### Target Detection



#### **MINIMUM DETECTABLE SIGNAL**

- THRESHOLD DETECTION:
- Threshold level is set at the output of Rx. If Rx output crosses the threshold, signal which is a mixture of echo and noise is assumed to represent a target



- Envelope (echo + noise) has fluctuating appearance because of random nature of Noise
- Envelope shown has passed through Matched filter which makes echoes no more look like rectangular pulses. They appear as triangular as shown in the graph
- Diagram shown is the combination of echo and noise. Threshold level is set such that noise alone does not cross the level and falsely taken as target

# Target A :

- Target A has large signal echo, greater than the surrounding noise amplitude and crosses threshold on its own and declared as a valid target without any ambiguity
- Let Target echoes of B &C are of equal voltage amplitude

# Target B :

Noise voltage amplitude at occurrence of signal is large. Signal echo combined with noise at that instant is just sufficient enough to cross the threshold and declared as a valid target 239

#### > Target C :

- Here the noise level is small at this instant of time the resultant of echo and noise signal does not cross the threshold level. So target presence is not declared. The target has missed being detected.
- Noise sometimes enhance the detection of weak echo signals

# **False Alarm:**

Weak signal C would not have been lost if threshold level is lower. But low threshold increases the likelihood of noise alone crossing the threshold and declared as a real target. This is called as False alarm.

#### **THRESHOLD DETECTION OF TARGET SIGNALS**



Time

#### Threshold level Setting:

- If threshold level is set too low so that weak echo signals also can be declared as valid targets, false targets are declared, since at some instant in time noise may cross the threshold level
- If threshold level is set too high, weak echoes are missed. Thus real targets are missed.
- Selection of threshold has to be done judiciously depending on the goals set in the design parameter.
   Probability of miss or Probability of false alarm

- Probability of Miss:
- Failing to indicate the presence of real target
- > Probability of False Alarm:
- Falsely indicating presence of target even though there is no real target

#### > Manual setting of Threshold by operator:

Probability of miss or Probability of False alarm depends on i) skill of operator ii) motivation of operator iii) state of operator's fatigue

# RECEIVER NOISE AND SIGNAL TO NOISE (S/N) RATIO

# **RECEIVER NOISE & S/N RATIO**

- Intub Discuss in detail the quantitative analysis
   of Receiver noise and hence derive expression for
   minimum detectable signal
- Image: Components
   Image: Describe different noise components
   present in radar systems
- Receiver noise: Noise interferes with detection of echo from target. i) Noise may exist within the Receiver itself. ii) Noise also enters the Receiver along with echo. Iii) Even if the radar is operated in a noise free environment, thermal noise still exists. Thermal noise is due to the thermal motion of electronics in the Receiver circuits

# **RECEIVER NOISE & S/N RATIO**

#### Thermal noise or Johnson Noise

- Noise that is generated due to thermal agitation of conduction electrons in the Ohmic portion of Receiver input stages is called Thermal Noise
- Thermal Noise Power (watts) = K T B<sub>n</sub>

K = Boltzmann's constant =  $1.38 \times 10^{-23}$ 

joules/degree

- T = Temperature in Degrees Kelvin
- $B_n$  = Noise Band width Hz

# **RECEIVER NOISE & S/N RATIO (CONTD..)**

# Ideal Receiver:

- ✤ i) No noise due to external source
- ✤ ii) Rx does not generate any noise
- ✤ iii) only Thermal noise is present

#### Practical Receiver :

- A practical Receiver has additional noise components other than thermal noise. Noise power of Practical Rx is greater than that from thermal noise alone
- ➢ Noise Figure : (F<sub>n</sub>)

 $F_n = \frac{\text{Noise output power of Practical Receiver}}{\text{Noise output of Ideal Receiver}}$ 

#### **RECEIVER NOISE & S/N RATIO (CONTD..)**

#### > Noise Figure:

**Noise output power of Practical Receiver**  $F_n =$ **Noise output of Ideal Receiver**  $= \frac{N_{out}}{K T_{O} B_{n} G_{A}}$  $N_{out}$  = Noise output of practical Rx  $G_A$  = Amplifier Gain =  $\frac{S_{out}}{S_{in}}$  $S_{in}$  = signal input of Rx,  $S_{out}$  = signal output of Rx  $T_0 = 290 \text{ K} (273 + 17) \text{ Room temp} = 17^0 \text{ C}$ B = Bandwidth of Receiver

#### **NOISE FIGURE**

• SIGNAL TO NOISE RATIO:



# **NOISE FIGURE (CONT)**

• Noise figure =  $F_n =$ 

Noise output of practical receiver Noise output of Ideal receiver

• 
$$F_n = \frac{N_{out}}{K T_0 B_N G_A}$$
  
 $F_n = \frac{N_{out}}{K T_0 B_N \frac{S_{out}}{S_{in}}} = \frac{N_{out}}{N_{in} \frac{S_{out}}{S_{in}}}$   
 $F_n = \frac{S_{in}}{N_{in}} \times \frac{1}{\frac{S_{out}}{N_{out}}} = \frac{\frac{S_{in}}{N_{in}}}{\frac{S_{out}}{N_{out}}}$ 

•  $F_n = \frac{\text{Input Signal to Noise Ratio}}{\text{output Signal to Noise Ratio}}$ 

# **NOISE FIGURE (CONT)**

- $F_n = \frac{\text{Input Signal to Noise Ratio}}{\text{output Signal to Noise Ratio}}$
- This means  $F_N$  is degradation in signal to noise ratio when signal passes through practical  $R_X$

#### **NOISE FIGURE (CONT)**

• 
$$F_n = \frac{\frac{S_{in}}{N_{in}}}{\frac{S_{out}}{N_{out}}}$$

• 
$$\frac{S_{in}}{N_{in}} = F_n \frac{S_{out}}{N_{out}} = F_n (S/N)_{out}$$

• 
$$S_{in} = N_{in} F_n (S/N)_{out} = K T_0 B_n F_n (S/N)_{out}$$

In limiting case S<sub>in</sub> becomes (S/N)<sub>in(min)</sub> and (S/N)<sub>out</sub> becomes (S/N)<sub>out(min)</sub>
 (S/N)<sub>in(min)</sub> = K T<sub>0</sub> B<sub>n</sub> F<sub>n</sub> (S/N)<sub>out(min)</sub>
### **Noise Figure (cont)**

• We know that (Radar equation)

• 
$$R_{\text{max}}^{4} = \frac{P_T G_T A_e \sigma}{(4 \pi)^2 S_{\text{min}}}$$

- But from the previous slide we have
- $(S/N)_{in(min)}$  =  $K T_0 B_n F_n (S/N)_{out(min)}$
- Combining the two above

• 
$$R_{max}^{4} = \frac{P_T G_T A_e \sigma}{(4 \pi)^2 K T_O B_n F_n (S/N)_{out(min)}}$$
  
•  $R_{max}^{4} = \frac{P_T G_T A_e \sigma}{(4 \pi)^2 K T_O B_n F_n (S/N)_{min}}$ 

• A low power, short range radar is solid state throughout, including a low noise RF amplifier which gives it an overall Noise Figure of 4.77 dB. If the antenna diameter is 1m, the IF bandwidth is 500 kHz, the operating frequency is 8 GHz and the radar set is supposed to be capable of detecting targets of 5 m<sup>2</sup> cross-sectional area at a maximum distance of 12 km, what must be the peak transmitted pulse power?

- Given parameters:
- $F_n = 4.77 \text{ dB} = \text{Antilog} \left(\frac{4.77}{10}\right) = 3$ D = 1 mt f = 8 GHz  $\sigma = 5 \text{ mt}^2$
- $R_{max} = 12 \text{ Km} = 12 \times 10^3 \text{ mts}$
- (S/N) =10 (assumed)
- K =  $1.38 \times 10^{-23}$  joules /degree
- $T_0 = 290$  Kelvin

•	$A_e = \frac{\pi D^2}{4} = \frac{3.14 \times 1^2}{4} = 0.785 \text{ mt}^2$
•	$\lambda = \frac{C}{f} = \frac{3 \times 10^8}{8 \times 10^9} = 0.0375  m$
•	$G = \frac{4 \pi A_e}{\lambda^2} = \frac{4 \times 3.14 \times 0.785}{0.0375^2} = 7011$
•	$R_{max}^{4} = \left[\frac{P_T G A_e \sigma}{(4 \pi)^2 K T_O B_n F_n (S/N)_{min}}\right]$
•	$(12 \times 10^3)^4 =$
	$P_{T} 7011 \times 0.785 \times 5$
	$\boxed{(4 \times 3.14)^2 \times 1.38 \times 10^{-23} \times 290 \times 500 \times 10^3 \times 3 \times 10}$
•	$P_{\rm T}$ = 7.13 W

# **CONTINUED IN RADAR 1 E**