



OPERATIONS RESEARCH

Subject code: A70352
Regulations: R15-JNTUH
Class: IV Year B. Tech MECH I Sem



Department of Mechanical Engineering
BHARAT INSTITUTE OF ENGINEERING AND
TECHNOLOGY
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OPERATIONS RESEARCH (A70352)

COURSE PLANNER

I. Course Objective & Relevance:

Operations Research (O.R.) is the application of advanced analytical methods to help make better decisions. Since its inception nearly 70 years ago, O.R. has contributed billions of dollars in benefits and savings to corporations, government, and the nonprofit sector.

Operations Research is often concerned with determining the maximum (of profit, performance, or yield) or minimum (of loss, risk, or cost) of some real-world objective. Originating in military efforts before World War II, its techniques have grown to concern problems in a variety of industries. Applications of O.R. are abundant in industry such as airlines, manufacturing companies, service organizations, military branches, and in government. The range of problems and issues to which field of O.R. has contributed insights and solutions are vast. Some of it includes scheduling airlines, both planes and crew, deciding the appropriate place to place new facilities such as a warehouse or factory, managing the flow of water from reservoirs, identifying possible future development paths for parts of the telecommunications industry, establishing the information needs and appropriate systems to supply them within the health service, and identifying and understanding the strategies adopted by companies for their information systems. Other major areas of O.R. applications include Computing and information technologies, Environment, energy, and natural resources, Financial engineering, Manufacturing, Service sciences, Supply chain management, Marketing Engineering, Policy modeling and public sector work, design optimization, Revenue management, Inventory control, optimal production planning and control, Transportation, Network optimization, Allocation problems, Facility location, Assignment Problems, Vehicle Routing, Transportation, Scheduling, Personnel staffing and Waiting Line models.

Operation Research encompasses a wide range of problem-solving techniques and methods applied in the pursuit of improved decision-making and efficiency, such as simulation, mathematical optimization, queuing theory and other stochastic-process models, Markov decision processes, econometric methods, data envelopment analysis, neural networks, expert systems, decision analysis, and the analytic hierarchy process. Nearly all of these techniques involve the construction of mathematical models that attempt to describe the system. Operational researchers faced with a new problem must determine which of these techniques are most appropriate given the nature of the system, the goals for improvement, and constraints on time and computing power. (Adapted from INFORMS)

II. Course purpose:

The course is intended to cover some of the analytical methods like Dynamic Programming, Simulation Methods, Linear Programming Methods, Transportation, Assignment, Sequencing, Replacement, Theory of Games, Analytical Waiting Lines and Inventory Models to help make better decisions.

III. Course Outcome:

1. Able to understand the advanced analytical methods like Dynamic Programming, Simulation Methods, Linear Programming Methods, Transportation, Assignment, Sequencing, Replacement, Theory of Games, Analytical Waiting Lines and Inventory Methods to help make better decisions.
2. Able to formulate the real life problem into an appropriate mathematical model.
3. Able to choose and apply the appropriate techniques to solve the formulated model.
4. Able to test the model and its solution.
5. Able to implement the solution.

IV. HOW PROGRAM OUTCOMES ARE ASSESSED



Program outcomes		Level	Proficiency assessed by
PO1	Ability to apply acquired knowledge of science and engineering fundamentals in problem solving.	3	Assignments and Exams
PO2	Ability to undertake problem identification, formulation and providing optimum solution in software applications.	3	Assignments and Exams
PO3	Ability to utilize systems approach in designing and to evaluate operational performance of developed software.	3	Assignments and Exams
PO4	Graduates will demonstrate an ability to identify, formulate and solve complex information technology related problems.	2	--
PO5	Graduate will be capable to use modern tools and packages available for their professional arena.	2	Assignments and Exams
PO6	Understanding of the social, cultural responsibilities as a professional engineer in a global context.	--	--
PO7	Understanding the impact of environment on engineering designs based on the principles of inter-disciplinary domains for sustainable development.	1	--
PO8	Ability to understand the role of ethics in professional environment and implementing them.	--	--
PO9	Competency in software development to function as an individual and in a team of multidisciplinary groups.	2	--
PO10	Ability to have verbal and written communication skills to use effectively not only with engineers but also with community at large.	2	--
PO11	Ought to have strong fundamentals in Information Technology and be able to have lifelong learning required for professional and individual developments.	1	--
PO12	Be able to design, implement and manage projects in Information Technology with optimum financial resources with, environmental awareness and safety aspects	--	Assignments and Exams

V. HOW PROGRAM SPECIFIC OUTCOMES ARE ASSESSED

Program Specific Outcomes (PSOs)	Level	Proficiency assessed by
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PSO 1	The student will be able to apply the knowledge of Mathematics, Sciences and engineering fundamentals to formulate, analyze and provide solutions for the problems related to Mechanical engineering and communicate them effectively to the concerned.	2	Lectures, Assignments
PSO 2	Design mechanical systems in various fields such as machine elements, thermal, manufacturing, industrial and inter-disciplinary fields by using various engineering/technological tools to meet the mercurial needs of the industry and society at large.	2	Projects
PSO 3	The ability to grasp the latest development, methodologies of mechanical engineering and posses competent knowledge of design process, practical proficiencies, skills and knowledge of programme and developing ideas towards research.	3	Guest Lectures

Pre-requisites:

1. Knowledge in basic manufacturing processes
2. Logical and analytical reasoning skills
3. Mathematical concepts concerning co-ordinate geometry, linear algebra, matrices and calculus
4. Basic Probability & Statistics
5. Numerical Methods – Finite Difference method

VI. Course Contents – As per JNTUH Syllabus:

UNIT – I: Introduction: Development – Definition – Characteristics and Phases – Types of models – Operations Research models – applications. **Allocation:** Linear Programming Problem Formulation – Graphical solution – Simplex method – Artificial variables techniques: Two-phase method, Big-M method.

UNIT – II: Transportation Problem: Formulation – Optimal solution – unbalanced transportation problem – Degeneracy. **Assignment Problem** – Formulation – Optimal solution - Variants of Assignment Problem – Traveling Salesman problem.

UNIT – III: Sequencing: Introduction – Flow –Shop sequencing – n jobs through two machines – n jobs through three machines – Job shop sequencing – two jobs through ‘m’ machines. **Replacement:** Introduction – Replacement of items that deteriorate with time – when money value is not counted and counted – Replacement of items that fail completely-Group replacement.

UNIT – IV: Theory of Games: Introduction – Terminology – Solution of games with saddle points and without saddle points – 2 x 2 games – dominance principle – m x 2 & 2 x n games – graphical method. **Inventory:** Introduction – Single item, Deterministic models – Purchase inventory models with one price break and multiple price breaks – Stochastic models – demand may be discrete variable or continuous variable – Single period model and no set up cost.

UNIT – V: Waiting Lines: Introduction – Terminology - Single Channel – Poisson arrivals and Exponential service times – with infinite population and finite population models – Multichannel – Poisson arrivals and exponential service times with infinite population.

Dynamic Programming: Introduction – Terminology-Bellman’s Principle of Optimality – Applications of dynamic programming- shortest path problem – linear programming problem. **Simulation:** Introduction, Definition, types of simulation models, Steps involved in the simulation process- Advantages and Disadvantages – applications of simulation to queuing and inventory.



Relevant syllabus for GATE:

Linear programming, simplex method, transportation, assignment, network flow models, simple queuing models, Deterministic Inventory control models.

Relevant syllabus for IES:

Linear Programming - Graphical and Simplex methods, Transportation and Assignment models. Single server Queuing model. Inventory control, EOQ model.

Lesson Plan:

Lecture No.	Week	Unit	TOPIC	Course Learning Outcomes	Reference
1	1	I	operations research-development-definition	Defined operations research and its development	A Course in Operations Research / S.D.Sharma-Kedarnath V
2			introduction ,phases, models in OR	Described phases, models in OR	
3			lpp-formulation example-minimization	Explained LPP formulation	
4			lpp-formulation example	Explained LPP formulation	
5	2		solving lpp using simplex method	Solved LP Problems	
6			simplex method -lpp, problems in simplex method	Solved LP Problems	
7			solving lpp using simplex method	Solved LP Problems	
8			problems in simplex method	Solved LP Problems	
9	3		artificial variable technique	Demonstrated artificial variable technique	
10			artificial variable technique	Demonstrated artificial variable technique	
11			big-M method	Explained big-M method	
12			big-M method	Explained big-M method	
13	4		big-M method problems	Solved big-M method problems	
14			big-M method problems	Solved big-M method problems	
15			solving lpp, two phase method	Solved Two phase method problems	
16			solving lpp by 2-phase method	Solved Two phase method problems	
17	5		two phase simplex method	Solved Two phase method problems	
18			solving LPP by 2-phase method	Solved Two phase method problems	
19			two phase method	Solved Two phase method problems	
20	6	II	transportation problem-introduction, methods	Described Transportation problem	Operations Research / S.D.Sharma-
21			Problem on VAM method	Solved Problem on VAM method	
22			problems on uv methods	Solved Problems on UV Methods	
23			problems on uv methods	Solved Problems on UV	



			Methods	
24		ASSIGNMENT PROBLEMS	Solved ASSIGNMENT problems	
25	7		Solved ASSIGNMENT problems	
26			solved travelling salesman problems	
27			solved travelling salesman problems	
I Mid Examinations (Week 9)				
28	7	III	Introduction –Flow –Shop sequencing	Described Flow Shop sequencing
29			Sequencing-n jobs 2 and 3 machine	Described Sequencing-n jobs 2 and 3 machine
30			Sequencing-n jobs 2 and 3 machine problems	Solved Sequencing-n jobs 2 and 3 machine problems
31	8	III	n jobs through three machines	Explained n jobs through three machines
32			Job shop sequencing – two jobs through ‘m’ machines.	Explained Job shop sequencing two jobs through ‘m’ machines.
33			Problems	Solved n jobs through three machines problems
34			Problems	Solved n jobs through three machines problems
35	9	III	Introduction to Replacement of items that deteriorate with time – when money value is not counted and counted	Described Replacement of items
36			Replacement of items that fail completely	Described Replacement of items that fail completely
37			Replacement Policy Type-1 Model	Explained Replacement Policy Type-1 Model
38			Type-1 Model PROBLEMS	Solved Type-1 Model PROBLEMS
39	10	III	Type II model	Explained Replacement Policy Type II Model
40			Type II model PROBLEMS	Solved Type II Model PROBLEMS
41			Type III model: group replacement	Explained group replacement
42			Type III model: group replacement PROBLEMS	Solved Group Replacement PROBLEMS
43	11	IV	THEORY OF GAMES : Introduction – Minimax (maximin) – Criterion and optimal strategy	Described THEORY OF GAMES
44			Solution of games with saddle points – Rectangular games without saddle points – 2 X 2 games –	Explained games with & without saddle points
45			dominance principle	Explained dominance

A Course in Operations Research / S.D.Sharma-KedarnathV

Operations Research / S.D.Sharma-



			principle		
46		m X 2 & 2 X n games	Explained m X 2 & 2 X n games		
47		graphical method	Explained graphical method		
48	12	PROBLEMS	Solved Problems on m X 2 & 2 X n games		
49		Poisson arrivals – exponential service times – with infinite population & finite population models	Described Poisson arrivals		
50		Problems on Poisson arrivals & exponential service times – with infinite population and finite population models	Solved Problems on Poisson arrivals		
51		Problems on Poisson arrivals & exponential service times – with infinite population and finite population models	Solved Problems on Poisson arrivals		
52	13	Multichannel – Poisson arrivals – exponential service times with infinite population single channel Poisson arrivals	Described Multichannel – Poisson arrivals		
53		Problems on Multichannel – Poisson arrivals – exponential service times with infinite population single channel Poisson arrivals	Solved Problems on Multichannel Poisson arrivals		
54		PROBLEMS	Solved Problems on Multichannel Poisson arrivals		
55	14	V	INVENTORY : Introduction – Single item – Deterministic models	Described Inventory models	A Course in Operations Research / S.D.Sharma-Kedarnath V
56			Purchase inventory models with one price break and multiple price breaks – shortages are not allowed	Explained Purchase inventory models	
57			Stochastic models – demand may be discrete variable or continuous variable. Instantaneous production. Instantaneous demand and continuous demand and no set up cost.	Explained Stochastic models	
58			SIMULATION : Definition – Types of simulation models phases of simulation– applications of simulation. Inventory and Queuing problems. Advantages and Disadvantages–Simulation Languages	Explained Simulation	
58			<i>DYNAMIC PROGRAMMING : Introduction – Bellman’s Principle of optimality.</i>	Explained Dynamic Programming	
59	15		Applications of dynamic programming- capital budgeting problem	Explained Applications of Dynamic Programming	



60		shortest path problem	Solved shortest path problem
61		linear programming problem	Solved linear programming problem

Suggested Books:

a. Textbooks:

1. J K Sharma, Operations Research, 4th edition, Macmillan India Limited, 2009.
2. S D Sharma, Operations Research, Kedarnath Ramnath Publishers, 1996.

b. Reference Books:

3. A M Natarajan, P Balasubramani, A Tamilarasi, Operations Research, Pearson Education Publishers, 2005.
4. P Ramamurthy, Operations Research, 2nd edition, New Age International Publications, 2007.
5. N V S Raju, Operations Research, 2nd edition, SMS Education Publications, 2011.
6. R Paneerselvam, Operations Research, 2nd edition, PHI Publications, 2006.
7. F S Hillier, G J Lieberman, Introduction to Operations Research, 9th edition, TMH Publications, 2010.
8. H. A. Taha, Introduction to Operations Research, 8th edition, PHI Publications, 2008.
9. H. M. Wagner, Principles of Operations Research, 1st edition, PHI Publications, 1969.
10. M S Bazaraa, J J Jarvis & H D Sherali, Linear Programming and Network Flows, 4th edition, Wiley Publications, 2009.

Question Bank:

Descriptive theory questions:

Unit –I

S. No.	Question	Blooms Taxonomy Level	Course Outcomes
UNIT-I			
1	a. Explain the applications of OR? b. Explain advantages of OR? c. Explain scope of OR?	Understanding	1,2
2	Let us consider a company making single product. The estimated demand for the product for the next four months are 1000,800,1200,900 respectively. The company has a regular time capacity of 800 per month and an overtime capacity of 200 per month. The cost of regular time production is Rs.20 per unit and the cost of overtime production is Rs.25 per unit. The company can carry inventory to the next month and the holding cost is Rs.3/unit/month the demand has to be met every month. Formulate a linear programming problem for the above situation.	Applying	1,5
3	Explain the terminology involved in formulating a linear programming problem?	Analysing	1,3
4	Solve the following LP problem graphically Maximize $z = -x_1 + 2x_2$ S.T $x_1 - x_2 \leq -1, -0.5x_1 - x_2 \leq 2, x_1, x_2 \geq 0$	Applying	1,5
5	Solve the following LP problem graphically. Maximize $z = 2x_1 + x_2$ S.T $x_1 + 2x_2 \leq 10, x_1 + x_2 \leq 6, x_1 - x_2 \leq 2, x_1 - 2x_2 \leq 1$ $x_1, x_2 \geq 0$	Applying	1,5



6	Solve the following LP problem using simplex method. Maximize $6x_1 + 8x_2$ S.T $x_1 + x_2 \leq 10, 2x_1 + 3x_2 \leq 25, x_1 + 5x_2 \leq 35$ $x_1, x_2 \geq 0$	Applying	1,5
7	Solve the following LPP by Big-M penalty method Minimize $z = 5x_1 + 3x_2$ S.T $2x_1 + 4x_2 \leq 12, 2x_1 + 2x_2 = 10, 5x_1 + 2x_2 \geq 10$ and $x_1, x_2 \geq 0$	Applying	1,5
8	Solve the following LPP by two phase method Minimize $z = 3x_1 + 4x_2$ S.T $2x_1 + 3x_2 \geq 8, 5x_1 + 2x_2 \geq 12, x_1, x_2 \geq 0$	Applying	1,5
9	a. Explain what is meant by degeneracy in LPP? How can this be solved? b. Solve the following LP problem by two phase method. Maximize $z = 5x_1 + 8x_2$ S.T $3x_1 + 2x_2 \geq 3$ $x_1 + 4x_2 \geq 4$ $x_1 + x_2 \leq 5$ $x_1 + x_2 \geq 0$	Applying	1,5
10	A firm produces three types of biscuits A,B,C it packs them in packets of two sizes 1 and 11. The size 1 contains 20 biscuits of type A, 50 of type B and 10 of type C. the size 11 contains 10 biscuits of the A, 80 of type B and 60 of type C. A buyer intends to buy at least 120 biscuits of type A, 740 of type B and 240 of type C. Determine the least number of packets he should buy. Write the dual LP problem and interrupt your answer.	Applying	1,5

UNIT-II

1	a. Write the general Mathematical model of transportation problem? b. What do you understand by degeneracy in a transportation problem?	Analysing	1,2																																			
2	A Company has three plants at locations A,B and C which supply to warehouses located at D,E,F,G and H. monthly plant capacities are 800,500 and 900 respectively. Monthly warehouse requirements are 400, 500,400 and 800 units respectively. Unit transportation cost in rupees are given below. <table border="1" style="margin-left: 20px;"> <tr> <td></td> <td>D</td> <td>E</td> <td>F</td> <td>G</td> <td>H</td> </tr> <tr> <td>A</td> <td>5</td> <td>8</td> <td>6</td> <td>6</td> <td>3</td> </tr> <tr> <td>B</td> <td>4</td> <td>7</td> <td>7</td> <td>6</td> <td>5</td> </tr> <tr> <td>C</td> <td>8</td> <td>4</td> <td>6</td> <td>6</td> <td>4</td> </tr> </table> Determine an optimum distribution for the company in order to minimize the total transportation cost by NWCR.		D	E	F	G	H	A	5	8	6	6	3	B	4	7	7	6	5	C	8	4	6	6	4	Applying	1,5											
	D	E	F	G	H																																	
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C	8	4	6	6	4																																	
3	Obtain initial solution in the following transportation problem by using VAM and LCM. <table border="1" style="margin-left: 20px;"> <tr> <td>Source</td> <td>D1</td> <td>D2</td> <td>D3</td> <td>D4</td> <td>D5</td> <td>Availability</td> </tr> <tr> <td>S1</td> <td>5</td> <td>3</td> <td>8</td> <td>6</td> <td>6</td> <td>1100</td> </tr> <tr> <td>S2</td> <td>4</td> <td>5</td> <td>7</td> <td>6</td> <td>7</td> <td>900</td> </tr> <tr> <td>S3</td> <td>8</td> <td>4</td> <td>4</td> <td>6</td> <td>6</td> <td>700</td> </tr> <tr> <td>Requirement</td> <td>800</td> <td>400</td> <td>500</td> <td>400</td> <td>600</td> <td></td> </tr> </table>	Source	D1	D2	D3	D4	D5	Availability	S1	5	3	8	6	6	1100	S2	4	5	7	6	7	900	S3	8	4	4	6	6	700	Requirement	800	400	500	400	600		Applying	1,5
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4	<p>A company has factories at F_1, F_2 and F_3 that supply products to ware houses at W_1, W_2 and W_3. The weekly capacities of the factories are 200,160 and 90 units. The weekly warehouse requirements are 180,120 and 150/units respectively. The unit shipping costs in rupees are as follows. Find the optimal solution</p>	Applying	1,5																																									
<table border="1"> <thead> <tr> <th></th> <th></th> <th>W_2</th> <th>W_3</th> <th>Supply</th> </tr> </thead> <tbody> <tr> <td>F_1</td> <td>16</td> <td>20</td> <td>12</td> <td>200</td> </tr> <tr> <td>F_2</td> <td>14</td> <td>8</td> <td>18</td> <td>160</td> </tr> <tr> <td>F_3</td> <td>26</td> <td>24</td> <td>16</td> <td>90</td> </tr> <tr> <td>Demand</td> <td>180</td> <td>120</td> <td>150</td> <td>450</td> </tr> <tr> <td></td> <td>0</td> <td>0</td> <td>0</td> <td></td> </tr> </tbody> </table>				W_2	W_3	Supply	F_1	16	20	12	200	F_2	14	8	18	160	F_3	26	24	16	90	Demand	180	120	150	450		0	0	0														
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5	<p>a. Write the Mathematical representation of an assignment model? b. Briefly explain about the assignment problems in OR and applications of assignment in OR?</p>	Analysing	1,5																																									
6	<p>Different machines can do any of the five required jobs, with different profits resulting from each assignments shown in the adjusting table. Find out maximum profit possible through optimal assignment.</p>	Applying	1,2																																									
<table border="1"> <thead> <tr> <th rowspan="2">Jobs</th> <th colspan="5">Machines</th> </tr> <tr> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>30</td> <td>37</td> <td>40</td> <td>28</td> <td>40</td> </tr> <tr> <td>2</td> <td>40</td> <td>24</td> <td>27</td> <td>21</td> <td>36</td> </tr> <tr> <td>3</td> <td>40</td> <td>32</td> <td>33</td> <td>30</td> <td>35</td> </tr> <tr> <td>4</td> <td>25</td> <td>38</td> <td>40</td> <td>36</td> <td>36</td> </tr> <tr> <td>5</td> <td>29</td> <td>62</td> <td>41</td> <td>34</td> <td>39</td> </tr> </tbody> </table>		Jobs	Machines					A	B	C	D	E	1	30	37	40	28	40	2	40	24	27	21	36	3	40	32	33	30	35	4	25	38	40	36	36	5	29	62	41	34	39		
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7	<p>A typical assignment problem, presented in the classic manner. Here there are five machines to be assigned to five jobs. The numbers in the matrix indicate the cost of doing each job with each machine. Jobs with costs of M are disallowed assignments. The problem is to find the minimum cost matching of machines to jobs.</p>	Applying	1,5																																									
<table border="1"> <thead> <tr> <th></th> <th>J1</th> <th>J2</th> <th>J3</th> <th>J4</th> <th>J5</th> </tr> </thead> <tbody> <tr> <td>M1</td> <td>M</td> <td>8</td> <td>6</td> <td>12</td> <td>1</td> </tr> <tr> <td>M2</td> <td>15</td> <td>12</td> <td>7</td> <td>M</td> <td>10</td> </tr> <tr> <td>M3</td> <td>10</td> <td>M</td> <td>5</td> <td>14</td> <td>M</td> </tr> <tr> <td>M4</td> <td>12</td> <td>M</td> <td>12</td> <td>16</td> <td>15</td> </tr> <tr> <td>M5</td> <td>18</td> <td>17</td> <td>14</td> <td>M</td> <td>13</td> </tr> </tbody> </table>			J1	J2	J3	J4	J5	M1	M	8	6	12	1	M2	15	12	7	M	10	M3	10	M	5	14	M	M4	12	M	12	16	15	M5	18	17	14	M	13							
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8	<p>A salesman has to visit five cities A,B,C,D,E. The intercity distances are tabulated below.</p>	Applying	1,5																																									
<table border="1"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>-</td> <td>12</td> <td>24</td> <td>25</td> <td>15</td> </tr> <tr> <td>B</td> <td>6</td> <td>-</td> <td>16</td> <td>18</td> <td>7</td> </tr> <tr> <td>C</td> <td>10</td> <td>11</td> <td>-</td> <td>18</td> <td>12</td> </tr> <tr> <td>D</td> <td>14</td> <td>17</td> <td>22</td> <td>-</td> <td>16</td> </tr> <tr> <td>E</td> <td>12</td> <td>13</td> <td>23</td> <td>25</td> <td>-</td> </tr> </tbody> </table> <p>Find the shortest route covering all the cities.</p>			A	B	C	D	E	A	-	12	24	25	15	B	6	-	16	18	7	C	10	11	-	18	12	D	14	17	22	-	16	E	12	13	23	25	-							
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UNIT-III

1	Explain the terminology of sequencing techniques in operations research?	Analysing	1,5																																			
2	<p>A book binder has one printing press, one binding machine and manuscripts of 7 different books. The time required for performing printing and binding operations for different books are shown below.</p> <table border="1"> <tr> <td>Book</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>Printingtime (hr)</td> <td>20</td> <td>90</td> <td>80</td> <td>20</td> <td>120</td> <td>15</td> <td>65</td> </tr> <tr> <td>Bindingtime(hrs)</td> <td>25</td> <td>60</td> <td>75</td> <td>30</td> <td>90</td> <td>35</td> <td>50</td> </tr> </table> <p>Decide the optimum sequence of processing of books in order to minimize the total time required to bring out all the books.</p>	Book	1	2	3	4	5	6	7	Printingtime (hr)	20	90	80	20	120	15	65	Bindingtime(hrs)	25	60	75	30	90	35	50	Applying	1,5											
Book	1	2	3	4	5	6	7																															
Printingtime (hr)	20	90	80	20	120	15	65																															
Bindingtime(hrs)	25	60	75	30	90	35	50																															
3	<p>Six jobs go first on machine A, then on machine B and last on machine C. The order of completion of jobs has no significance. The following table gives machine time for the six jobs and the three machines. Find the sequence of jobs that minimizes elapsed time to complete the jobs.</p> <table border="1"> <thead> <tr> <th rowspan="2">Jobs</th> <th colspan="3">Processing Time</th> </tr> <tr> <th>Machine A</th> <th>Machine B</th> <th>Machine C</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>8</td> <td>3</td> <td>8</td> </tr> <tr> <td>2</td> <td>3</td> <td>4</td> <td>7</td> </tr> <tr> <td>3</td> <td>7</td> <td>5</td> <td>6</td> </tr> <tr> <td>4</td> <td>2</td> <td>2</td> <td>9</td> </tr> <tr> <td>5</td> <td>5</td> <td>1</td> <td>10</td> </tr> <tr> <td>6</td> <td>1</td> <td>6</td> <td>9</td> </tr> </tbody> </table>	Jobs	Processing Time			Machine A	Machine B	Machine C	1	8	3	8	2	3	4	7	3	7	5	6	4	2	2	9	5	5	1	10	6	1	6	9	Applying	1,5				
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4	<p>Solve the following sequence problem, given an optimal solution when passing is not allowed.</p> <table border="1"> <thead> <tr> <th rowspan="2">Machines</th> <th colspan="5">Jobs</th> </tr> <tr> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <td>M1</td> <td>11</td> <td>13</td> <td>9</td> <td>16</td> <td>17</td> </tr> <tr> <td>M2</td> <td>4</td> <td>3</td> <td>5</td> <td>2</td> <td>6</td> </tr> <tr> <td>M3</td> <td>6</td> <td>7</td> <td>5</td> <td>8</td> <td>4</td> </tr> <tr> <td>M4</td> <td>15</td> <td>8</td> <td>13</td> <td>9</td> <td>11</td> </tr> </tbody> </table>	Machines	Jobs					A	B	C	D	E	M1	11	13	9	16	17	M2	4	3	5	2	6	M3	6	7	5	8	4	M4	15	8	13	9	11	Applying	1,5
Machines	Jobs																																					
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M4	15	8	13	9	11																																	
5	<p>A firm is considering the replacement of a machine, whose cost price is Rs.12,200 and its shop value is Rs.200. From experience the running (maintenance and operating) costs are found to be as follows.</p> <table border="1"> <tr> <td>Year</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <td>Runningcost</td> <td>200</td> <td>500</td> <td>800</td> <td>1200</td> <td>1800</td> <td>2500</td> <td>3200</td> <td>4000</td> </tr> </table> <p>When should the machine be replaced?</p>	Year	1	2	3	4	5	6	7	8	Runningcost	200	500	800	1200	1800	2500	3200	4000	Applying	1,2																	
Year	1	2	3	4	5	6	7	8																														
Runningcost	200	500	800	1200	1800	2500	3200	4000																														
6.	<p>The management of a large hotel is considering the periodic replacement of light bulbs fitted in it's room .There are 500 rooms in the hotel and each room has 6 bulbs. The management is now following the policy of replacing the bulbs as they fail at the total cost of Rs:3 per bulb .The management feels that this cost can be reduced to Rs:1 by adopting the group replacement method. On the basis of the information given below, evaluate The alternative and make a recommendation to the management</p> <table border="1"> <tr> <td>Month of use</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>Percent of bulbs failing by that month</td> <td>10</td> <td>25</td> <td>50</td> <td>80</td> <td>100</td> </tr> </table>	Month of use	1	2	3	4	5	Percent of bulbs failing by that month	10	25	50	80	100	Applying	1,5																							
Month of use	1	2	3	4	5																																	
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7	The data collected in running a Machine the cost of which is Rs:60,000 are given below	Applying	1,2																								
<table border="1"> <tr> <td>Resale value</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>Resale value (Rs)</td> <td>42,000</td> <td>30,000</td> <td>20,400</td> <td>14,400</td> <td>9,650</td> </tr> <tr> <td>Cost of Spares (Rs)</td> <td>4,000</td> <td>4,270</td> <td>4,880</td> <td>5,700</td> <td>6,800</td> </tr> <tr> <td>Cost of Labour</td> <td>14,000</td> <td>16,000</td> <td>18,000</td> <td>21,000</td> <td>25,000</td> </tr> </table> <p>Find the time when the machine should be replaced?</p>		Resale value	1	2	3	4	5	Resale value (Rs)	42,000	30,000	20,400	14,400	9,650	Cost of Spares (Rs)	4,000	4,270	4,880	5,700	6,800	Cost of Labour	14,000	16,000	18,000	21,000	25,000		
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Cost of Labour	14,000	16,000	18,000	21,000	25,000																						

8	Machine A costs Rs:45,000 and it's operating costs are estimated to be Rs:1,000 for the first year increasing by Rs:10,000 per year in the second year and subsequent years .Machine B costs Rs:50,000 and operating cost are Rs:2,000 for the first year and increasing by Rs:4,000 in the second and subsequent years. If at present we have a machine of type A, should we replace it with B? If so when? Assume both machines have no resale value and this future cost are not discounted?	Applying	1,5
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9	Machine A costs of Rs:80,000. Annually operating cost are Rs:2,000 for the first years and they increase by Rs:15,000 every years (for example in the fourth year the operating cost are Rs:47,000).Determine the least age at which to replace the machine. If the optional replacement policy is followed. (a)What will be the average yearly cost of operating and owing the machine (Assume that the reset value of the machine is zero when replaced, and that future costs are not discounted.Another machine B cost Rs:1,00,000.Annual operating cost for the first year is Rs:4,000 and they increase by Rs:7,000 every year .The following firm has a machine of type A which is one year old. Should the firm replace it with B and if so when? Suppose the firm is just ready to replace the M/c A with another M/c of the same type, just the the firm gets an information that the M/c B will become available in a year .What should firmdo?	Applying	1,5
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UNIT-IV

1	(a)Explain two person zero sum game and npersongame? (b)Explain pay of matrix and types of strategy in game theory?	Understanding	1,2
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2	Solve the following game	Applying	1,5														
<table border="1"> <tr> <td></td> <td colspan="3" style="text-align: center;">B</td> </tr> <tr> <td rowspan="3" style="text-align: center;">A</td> <td>5</td> <td>20</td> <td>-10</td> </tr> <tr> <td>10</td> <td>6</td> <td>2</td> </tr> <tr> <td>20</td> <td>15</td> <td>18</td> </tr> </table>			B			A	5	20	-10	10	6	2	20	15	18		
	B																
A	5	20	-10														
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	20	15	18														

3	Solve the following game	Applying	1,5												
<table border="1"> <tr> <td></td> <td>Y1</td> <td>Y2</td> <td>Y3</td> </tr> <tr> <td>X1</td> <td>4</td> <td>20</td> <td>6</td> </tr> <tr> <td>X2</td> <td>18</td> <td>12</td> <td>10</td> </tr> </table>			Y1	Y2	Y3	X1	4	20	6	X2	18	12	10		
	Y1	Y2	Y3												
X1	4	20	6												
X2	18	12	10												

4	Using the dominance property obtain the optimal strategy for both the players and determine the value of game. The payoff matrix for player A is given	Applying	1,2																								
<table border="1"> <tr> <td></td> <td colspan="5" style="text-align: center;">PLAYER -B</td> </tr> <tr> <td></td> <td>I</td> <td>II</td> <td>III</td> <td>IV</td> <td>V</td> </tr> <tr> <td>I</td> <td>2</td> <td>4</td> <td>3</td> <td>8</td> <td>4</td> </tr> <tr> <td>II</td> <td>5</td> <td>6</td> <td>8</td> <td>7</td> <td>8</td> </tr> </table>			PLAYER -B						I	II	III	IV	V	I	2	4	3	8	4	II	5	6	8	7	8		
	PLAYER -B																										
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I	2	4	3	8	4																						
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		III	6	7	9	8	7																												
	PLAYER A	IV	4	2	8	4	3																												
5	Find the range of value of P and Q that will render the entry (2,2) a saddle point for the following game	<p style="text-align: center;">PLAYER-B</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>B1</td> <td>B2</td> <td>B3</td> </tr> <tr> <td>A1</td> <td>2</td> <td>4</td> <td>5</td> </tr> <tr> <td>A2</td> <td>10</td> <td>7</td> <td>9</td> </tr> <tr> <td>A3</td> <td>4</td> <td>P</td> <td>6</td> </tr> </table>								B1	B2	B3	A1	2	4	5	A2	10	7	9	A3	4	P	6	Applying	1,2									
	B1	B2	B3																																
A1	2	4	5																																
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A3	4	P	6																																
6	A company is currently involved in negotiation with its union on the upcoming wage contract positive signs in the table represent wage increase while negative sign represents wage reduction what are the optimal strategies for the company as well as the union ? what is the game value?	<table style="margin-left: auto; margin-right: auto;"> <tr> <td colspan="5" style="text-align: center;">Union Strategy</td> </tr> <tr> <td>C1</td> <td>0.25</td> <td>0.27</td> <td>0.35</td> <td>-0.02</td> </tr> <tr> <td>C2</td> <td>0.20</td> <td>0.16</td> <td>0.08</td> <td>0.08</td> </tr> <tr> <td>C3</td> <td>0.14</td> <td>0.12</td> <td>0.15</td> <td>0.03</td> </tr> <tr> <td>C4</td> <td>0.30</td> <td>0.14</td> <td>0.19</td> <td>0.00</td> </tr> </table>							Union Strategy					C1	0.25	0.27	0.35	-0.02	C2	0.20	0.16	0.08	0.08	C3	0.14	0.12	0.15	0.03	C4	0.30	0.14	0.19	0.00	Applying	1,5
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C4	0.30	0.14	0.19	0.00																															
7	Two breakfast food manufacturers ABC and XYZ are competing for an increased market share. The pay off matrix, shown in the following table describes the increase in market share for ABC and decrease in market share Of XYZ.	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>ABC</td> <td>Give coupons</td> <td>Dec price</td> <td>Maintain present strategy</td> <td>Increase and advertizing</td> </tr> <tr> <td>Give coupons</td> <td>2</td> <td>-2</td> <td>4</td> <td>1</td> </tr> <tr> <td>Decrease price</td> <td>6</td> <td>1</td> <td>12</td> <td>3</td> </tr> <tr> <td>Maintain present strategy</td> <td>-3</td> <td>2</td> <td>0</td> <td>6</td> </tr> <tr> <td>Increase adv</td> <td>2</td> <td>-3</td> <td>7</td> <td>1</td> </tr> </table>							ABC	Give coupons	Dec price	Maintain present strategy	Increase and advertizing	Give coupons	2	-2	4	1	Decrease price	6	1	12	3	Maintain present strategy	-3	2	0	6	Increase adv	2	-3	7	1	Applying	1,5
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8	Use the graphical method for solving the following game and find the value of the game	<table style="margin-left: auto; margin-right: auto;"> <tr> <td colspan="6" style="text-align: center;">Player-B</td> </tr> <tr> <td></td> <td>B1</td> <td>B2</td> <td>B3</td> <td>B4</td> <td>Probability</td> </tr> <tr> <td>A1</td> <td>2</td> <td>2</td> <td>3</td> <td>-2</td> <td>P1</td> </tr> <tr> <td>A2</td> <td>4</td> <td>3</td> <td>2</td> <td>6</td> <td>P2</td> </tr> </table>							Player-B							B1	B2	B3	B4	Probability	A1	2	2	3	-2	P1	A2	4	3	2	6	P2	Applying	1,5	
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A1	2	2	3	-2	P1																														
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9	What are inventory models? Enumerate various types of inventory models and describe them briefly	Understanding							1,5																										
10	The production department of a company required 3,600kg of raw material for manufacturing a particular item per year. It has been estimated that the cost of placing an order is Rs.36 and the cost of carrying inventory is 25% of the investment in the inventories, the price is Rs.10/kg. help the purchase manager to determine and ordering policy for raw material, determine optimal lot size	Applying							1,5																										



11	Purchase manager places order each time for a lot of 500 no of particular item from the available data the following results are obtained, inventory carrying 40%, ordering cost order Rs.600, cost per unit Rs.50 annual demand 1000, find out the loser to the organization due to his policy.	Applying	1,5
12	A dealer supplies you the following information with regards to an product that he deals in annual demand =10,000 units, ordering cost Rs.10/order, Price Rs.20/unit. Inventory carrying cost is 20% of the value of inventory per year. The dealer is considering the possibility of allowing some back orders to occurs. He has estimated that the annual cost of back ordering will be 25% of the value of inventory. a. What should be the optimum no of units he should buy in 1lot? b. What qty of the product should be allowed to be backordered c. What would be the max qty of inventory at any time of year Would you recommend to allow backordering? If so what would be the annual cost saving by adopting the policy of backordering.	Applying	1,5
13	The annual demand of a product is 10,000 units. Each unit costs Rs.100 if the orders are placed in quantities below 200 units. for orders above 200 or above, however the price is Rs.95. The annual inventory holding costs is 10% of the value of the item and the ordering costs is Rs.5/order. Find economic lot size?	Applying	1,5
14	Find the optimal economical order Qty for a product having the following characteristics. Annual demand 2400 units, ordering cost C_0 =Rs 100 lost of storage C_h =24% of unit cost price break Qty $0 \leq Q < 500$ $500 \leq Q$ Price /unit (Rs) Rs.10 Rs.900	Applying	1,5

UNIT V

1	Explain the terms Balking, Reneging, Jockeying.	Understand	1,5
2	Explain the terms single server and multiple server que length and finite and Infinite que length.	Understand	1,5
3	Customers arrive at box office windows being manned by a single individual, according to a poisson input process with a mean rate of 20/hr. the time required to seme a customer has an exponential distribution with a mean of 90 sec. Find the avg waiting time of customers. Also determine the avg number of customers in the system and avg queue length.	Applying	1,2
4	A road transport company has one reservation clerk on duty at a time. He handles information of bus schedules and makes reservations customers arrive at a rate of 8 per hour and the clerk can, on an average, service 12 customers per hour. After starting your assumptions determine. a. What is the avg number of customer waiting for the service of the clerk b. What is the avg time a customer has to wait before being used?	Applying	1,5



5	Consider a single server queuing system with poisson input and exponential service times. Suppose that mean arrival rate is 3 calling units per hour, the expected service time is 0.25 hours and the maximum permissible calling units in the system is two. Derive the steady state probability distribution of the number of calling units in the system. And then calculate the expected number in the system.	Applying	1,5
6	At a railway station only one train is handled at a time. The railway track is sufficient only for two trains to wait while others are given signal to leave the station. Trains arrive at the station at an average rate of 6 per/hours and the railway station can handle them on an average of 12 per/hours. Assuming poisson arrivals and exponential service distribution find the steady state probability of the various numbers of trains in the system. also find the average number of trains in the system.	Applying	1,5
7	Explain the application of Queuing systems?	Understanding	1,5
8	In a departmental store one cashier is there to serve the customers. And the customers pick up their needs by themselves the arrival rate is 9 customers for every 5 minutes and the cashier can serve 10 customers in 5 minutes. Assuming poisson arrival rate and exponential distribution for service rate. Find a. Average number of customers in the system b. Average number of customers in the queue of average queue length? c. Average time a customer spends in the systems Average time a customer waits before being served.	Applying	1,5
9	A bank has two tellers working on the savings accounts. The first teller only handles withdrawals. The second teller only handles deposits. It has been found that the service time distributions for the deposits and withdrawals both are exponential with mean service time 3 min per customer. Depositors are found to arrive in a poisson fashion throughout the day with a mean arrival rate of 16/hr withdrawals also arrive in a poisson fashion with a mean arrival rate of 14/hr. what would be the effect on the average waiting time for depositors and withdrawals if each teller could handle both the withdrawals and deposits what would be the effect if this could only be accomplished by increasing the service time to 3.5 minutes?	Applying	1,2
10	A television repairman finds that the time spent on his jobs has an exponential distribution with a mean of 30 minutes. If he repairs the sets in the order in which they came in, and if the arrival of sets follows a poisson distribution with an approximate average rate of 10 per 8 hour day, what is the repairman's expected idle time each day? How many jobs are ahead of the average, set just brought in?	Applying	1,5
11	Use dynamic programming to solve the following problem Maximize $z = x_1^2 + 2x_2^2 + 4x_3^2$ S.T $x_1 + 2x_2 + x_3 \leq 8$ and $x_1, x_2, x_3 \geq 0$	Applying	1,2
12	Use dynamic programming to solve the following problem Maximize $z = x_1^2 + 2x_2^2 + 4x_3^2$ S.T $x_1 + 2x_2 + x_3 \leq 8$	Applying	1,2
13	Use Bell man's principle of optimality to find the optimum solution to the following problem. Minimize $z = y_1^2 + y_2^2 + y_3^2$ S.T $y_1 + y_2 + y_3 \geq 15$, $y_1, y_2, y_3 \geq 0$	Applying	1,5



14	Discuss dynamic programming with suitable examples?	Understanding	1,5																				
15	Solve the following LP problem by dynamic programming approach. Maximize $z = 8x_1 + 7x_2$ S.T $2x_1 + x_2 \leq 8, 5x_2 + 2x_1 \leq 15, x_1, x_2 \geq 0$	Applying	1,5																				
16	Use dynamic programming to solve the following LPP Maximize $z = 3x_1 + 5x_2$ S.T $x_1 \leq 4, x_2 \leq 6, 3x_1 + 2x_2 \leq 18, x_1, x_2 \geq 0$	Applying	1,5																				
17	Max $z = 3x_1 + 4x_2$ S.T $2x_1 + x_2 \leq 40, 2x_1 + 5x_2 \leq 180, x_1, x_2 \geq 0$ solve using dynamic programming.	Applying	1,5																				
18	Solve using dynamic programming Max $z = 50x_1 + 100x_2$ S.T $2x_1 + 3x_2 \leq 48, x_1 + 3x_2 \leq 42$ $x_1, x_2 \leq 21, x_1, x_2 \geq 0$	Applying	1,5																				
19	Solve using dynamic programming Max $z = 3x_1 + 5x_2$ S.T $x_1 \leq 4, x_2 \leq 6, 3x_1 + 2x_2 \leq 18, x_1, x_2 \geq 0$	Applying	1,5																				
20	What is simulation? Discuss application of simulation?	Understanding																					
21	Discuss the advantages and disadvantages of simulation.	Understanding	1,5																				
22	Define simulation why simulation uses. Give one application area when this technique is used in practice.	Understanding	1,5																				
23	Explain what factors must be considered when designing simulation experiment.	Understanding	1,5																				
24	Draw a flow chart to describe the simulation of a simple system.	Understanding	1,5																				
25	Discuss types of simulations?	Understanding	1,5																				
26	A company manufactures around 200 mopeds. Depending upon the availability of raw materials and other conditions. The daily production has been varying from 196 mopeds to 204 mopeds. Whose probability distribution are given below: <table border="1" style="margin-left: 20px;"> <tr> <td>Pro/day</td> <td>196</td> <td>197</td> <td>198</td> <td>199</td> <td>200</td> <td>201</td> <td>202</td> <td>203</td> <td>204</td> </tr> <tr> <td>Probability</td> <td>0.05</td> <td>0.09</td> <td>0.12</td> <td>0.14</td> <td>0.20</td> <td>0.15</td> <td>0.11</td> <td>0.08</td> <td>0.06</td> </tr> </table> <p>Finished mopeds are transported to a lorry that can accommodate only 200 mopeds. Random numbers are 82,89,78,24,53,61,18,45,04,23,50,77,54 and 10. Simulate the mopeds waiting.</p>	Pro/day	196	197	198	199	200	201	202	203	204	Probability	0.05	0.09	0.12	0.14	0.20	0.15	0.11	0.08	0.06	Applying	1,2
Pro/day	196	197	198	199	200	201	202	203	204														
Probability	0.05	0.09	0.12	0.14	0.20	0.15	0.11	0.08	0.06														
27	A bakery keeps stock of a popular brand of cake. Previous experience show the daily demand pattern for the item with associated probabilities as given <table border="1" style="margin-left: 20px;"> <tr> <td>Daily demand (number)</td> <td>0</td> <td>10</td> <td>20</td> <td>30</td> <td>40</td> <td>50</td> </tr> <tr> <td>Probability</td> <td>0.01</td> <td>0.20</td> <td>0.15</td> <td>0.50</td> <td>0.12</td> <td>0.02</td> </tr> </table> <p>use the following sequence of random numbers to simulate the demand for</p>	Daily demand (number)	0	10	20	30	40	50	Probability	0.01	0.20	0.15	0.50	0.12	0.02	Applying	1,5						
Daily demand (number)	0	10	20	30	40	50																	
Probability	0.01	0.20	0.15	0.50	0.12	0.02																	



	next 10 days. Random numbers: 25,39,65,76,12,05,73,89,19,49 Also estimate the daily average demand for the cakes on the basis of the simulated data		
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a. Objective questions

JNTUH

Unit-I

- 1) _____ as a field, primarily has a set or collection of algorithms which act as tools for problem solving in chosen application areas.
(a) Linear Program (b) Operations Research (c) Graphical Research (d) None of these
- 2) The scientific method in OR study generally involves:
(a) Judgment phase, (b) Research phase, (c) Action phase, (d) All of the above
- 3) Graphs are an example of _____.
(a) Iconic model, (b) Analogue model, (c) Symbolic model, (d) None of the above
- 4) Characteristic of OR is _____.
(a) Interdisciplinary, (b) Wholistic, (c) Scientific and Objective, (d) All of the above
- 5) The _____ is an abstraction of reality.
- 6) The scaled version of a real object is called _____.
- 7) Example of a Predictive OR model is _____ models.
- 8) Example of a Prescriptive OR model is _____ models.
- 9) Example of an Analogue OR model is _____ problem.
- 10) The number of phases in OR are _____.
- 11) Monte-Carlo Method is used to solve _____ models.
- 12) _____ is an application of matrix algebra used to solve a broad class of problems that can be represented by a system of linear equations.
- 13) If the objective and constraint functions are all linear, then the problem is called as ____.
- 14) The _____ method is limited to LP problems involving two decision variables and a limited number of constraints due to the difficulty of graphing and evaluating more than two decision variables.
- 15) The _____ method is much more powerful than the graphical method and provides optimal solution to LP problems containing thousands of decision variables and constraints.
- 16) The _____ of handling instances with artificial variables is the commonsense approach.
- 17) A LPP may be defined as the problem of maximizing or minimizing a linear function subject to _____.
- 18) A typical mathematical program consists of a single objective function, representing either a profit to be maximized or a cost to be minimized, and a set of constraints that circumscribe the _____.
- 19) The number of decision variables in graphical method of optimization is _____.
- 20) Pivot column is associated with _____ variable in simplex method.

Unit-II

- 1) The transportation model deals with shipment of commodity from _____ to _____.
- 2) The method of penalties is also called as _____ method.
- 3) The column, which is introduced in the matrix to balance the rim requirements, is _____.
- 4) Transportation problem where the demand or requirement is equals to the available resource is known as _____.



- 5) When the total allocations in transportation model of $m \times n$ size is not equals to $m + n - 1$ then the situation is known as _____.
- 6) VAM stands for _____.
- 7) Modified Distribution Method can be called as _____ method.
- 8) The cost of dummy cells is taken as _____ in TP.
- 9) A loop drawn in method of optimizing TP should consist of at least _____ corners.
- 10) The transportation model is treated as balanced if _____. (a) Demand = Supply (b) Demand > Supply (c) Demand < Supply (d) None
- 11) When the dual is feasible, we have reached the optimal solution to both primal and dual, therefore _____ method is optimal. (a) VAM (b) MODI (c) NWCM (d) Johnson
- 12) To convert the transportation problem into a maximization model we have to _____. (a) To write the inverse of the matrix (b) To multiply the rim requirements by -1 (c) To multiply the matrix by -1 (d) cannot convert the transportation problem in to a maximization problem, as it is basically a minimization problem.
- 13) The supply at three sources is 50, 40 and 60 units respectively whilst the demand at the four destinations is 20, 30, 10 and 50 units. In solving this transportation problem _____. (a) a dummy source of capacity 40 units is needed (b) a dummy destination of capacity 40 units is needed (c) no solution exists as the problem is infeasible (d) none solution exists as the problem is degenerate.
- 14) In Northwest corner method the allocations are made _____. (a) Starting from the left hand side top corner, (b) Starting from the right hand side top corner (c) Starting from the lowest cost cell (d) Starting from the lowest requirement and satisfying first.
- 15) In transportation model the optimality test can be carried out by: (a) Stepping Stone Method, (b) Modified Distribution Method, (c) both (a) & (b), (d) None

Unit-III

- 1) The fundamental assumption of Johnson's method of sequencing is _____.
- 2) If a job has zero processing time for any machine, the job must be processed _____.
- 3) In 2 jobs by m machine sequencing problem _____ is fixed.
- 4) In 2 jobs by m machine sequencing, a line at 45° represents: (a) Job 1 is idle, (b) Job 2 is idle, (c) Both jobs are idle, (d) No job is idle.
- 5) In sequencing, an optimal path is one that minimizes (a) Elapsed time, (b) Idle time, (c) Processing time, (d) Ready time.
- 6) In jobs A to D have process times as 5, 6, 8, 4 on first machine and 4, 7, 9, 10 on second machine, then the optimal sequence is: (a) CDAB, (b) ABCD, (c) BCDA, (d) DBCA.
- 7) The fundamental assumption for Johnson's algorithm of sequencing is _____ rule.
- 8) In n jobs by 2 machine sequencing problem, if two jobs J1 and J2 have equal processing times on both machines M1 and M2, then we can choose sequence _____.
- 9) The objective of sequencing problem is _____. (a) To find the order in which jobs are to be made (b) To find the time required for completing all the jobs on hand. (c) To find the sequence in which jobs on hand are to be processed to minimize the total time required for processing the jobs. (d) To maximize the effectiveness.
- 10) If there are 'n' jobs and 'm' machines, there will be _____ sequences of doing the jobs. (a) $n \times m$, (b) $(n!)^m$, (c) n^m (d) $(n!)^m$
- 11) In general sequencing problem will be solved by using _____. (a) Hungarian Method. (b) Simplex method. (c) Johnson and Bellman method, (d) Flood's technique.
- 12) In solving 2 machine and 'n' jobs, the following assumption is wrong: (a) No passing is allowed (b) Processing times are known, (c) Handling time is negligible, (d) The time of processing depends on the order of machining.



- 13) The following is one of the assumptions made while sequencing 'n' jobs on 2 machines:
(a) Two jobs must be loaded at a time on any machine. (b) Jobs are to be done alternatively on each machine. (c) The order of completing the jobs has high significance. (d) Each job once started on a machine is to be performed up to completion on that machine.
- 14) This is not allowed in sequencing of 'n' jobs on two machines: (a) Passing, (b) loading (c) Repeating the job (d) Once loaded on the machine it should be completed before removing from the machine.
- 15) At petrol Bunk, when 'n' vehicle are waiting for service then the service rule used is _____. (a) LIFO (b) FIFO (c) Service in Random Order (d) Service by highest profit
- 16) In replacement analysis, the maintenance cost is a function of _____.
- 17) When money value changes with time @ r, then discount factor for nth year = _____.
- 18) _____ cost refers to uniform annual equivalent loss in capital.
- 19) Running cost refers to uniform annual equivalent amount to be spent to _____ and _____ the equipment.
- 20) Replacement decision is very much common in _____ stage.

Unit-IV

- 1) If the value of the game is zero, then the game is known as _____.
- 2) When the game is played on a predetermined course of action, which does not change throughout game, then the game is said to be _____.
- 3) If the losses of player A are the gains of the player B, then the game is known as _____.
- 4) If there are more than two persons in a game then the game is known as _____.
- 5) The list of courses of action with each player is called _____.
- 6) The corresponding strategy of each player at equilibrium point is _____ strategy.
- 7) If minimax value is equal to maximin value, then the game is said to have _____.
- 8) Ram and Shyam play a game with two types of coins 5 ps and 10 ps. Each draws one coin randomly and if the sum is even Ram wins the coins, otherwise Shyam. The value of the game is _____.
- 9) The game whose payoff matrix is null matrix is _____ game.
- 10) The games with saddle points are: (a) Probabilistic in nature, (b) Normative in nature (c) Stochastic in nature, (d) Deterministic in nature.
- 11) When Minimax and Maximin criteria matches, then _____. (a) Fair game exists. (b) Unfair game exists, (c) Mixed strategy exists (d) Saddle point exists.
- 12) Identify the wrong statement: (a) Game without saddle point is probabilistic (b) Game with saddle point will have pure strategies (c) Game with saddle point cannot be solved by dominance rule. (d) Game without saddle point uses mixed strategies.
- 13) In case, there is no saddle point in a game then the game is: (a) Deterministic game, (b) Fair game, (c) Mixed strategy game, (d) Multi player game.
- 14) In case, there is no saddle point in a game then the game is: (a) Deterministic game, (b) Fair game, (c) Mixed strategy game, (d) Multi player game.
- 15) When there is dominance in a game then: (a) Least of the row \geq highest of another row (b) Least of the row \leq highest of another row (c) Every element of a row \geq corresponding element of another row. (d) Every element of the row \leq corresponding element of another row.
- 16) When the game is not having a saddle point, then the following method cannot be used to solve the game: (a) Linear Programming method, (b) Minimax and maximin criteria (c) Algebraic method (d) Graphical method.
- 17) A competitive situation is known as _____. (a) Competition (b) Marketing (c) Game (d) None of the above.



- 18) Theory of games and economic behavior was published by _____. (a) John Von Neumann and Morgenstern (b) John Flood (c) Bellman and Neumann (d) A K Erlang
- 19) A necessary and sufficient condition for a saddle point to exist is the presence of a _____ element which is both a minimum of its row and a maximum of its column. (a) payoff (b) 2 x 2 matrix (c) n x 2 matrix (d) 2 x m matrix
- 20) Stock level at which fresh order should be placed is known as _____.

Unit-V

- 1) The period between two successive arrivals is called _____.
- 2) Service distribution represents the _____ in which the number of customers leaves the system.
- 3) At a gas filling station, mean arrival rate is Poisson at 3 per hr and mean filling time is distributed exponentially at 10 min. Then the expected number of units in the system is _____.
- 4) The customer move from one queue will be tempted to join another queue because of its smaller size is known as _____.
- 5) A lottery system follows _____ queue discipline.
- 6) Waiting line problem arise because of _____. (a) Too much demand, (b) Too less demand, (c) both (a) & (b), (d) None
- 7) A queuing model is called multi-server model if the system has number of parallel channels each with server: (a) 1, (b) 0, (c) > 1, (d) None
- 8) If the number of arrivals during a given time period is independent of the number of arrivals that have already occurred prior to the beginning of time interval, then the new arrivals follow _____ distribution.
- 9) The characteristics of queue model are independent of: (a) Service pattern (b) Number of service points (c) Limit of queue, (d) Queue discipline
- 10) A customer leaving the queue thinking that he may not get service due to the lengthy queue is called _____. (a) Balker (b) Reneger (c) Jockeyer (d) Dissatisfied
- 11) As per queue discipline the following is not a negative behavior of a customer: (a) Balking (b) Reneging (c) Boarding (d) Collusion.
- 12) The expediting or follow up function in production control is an example of _____. (a) LIFO (b) FIFO (c) SIRO (d) Pre emptive.
- 13) In M/M/S: N/FIFO the following does not apply: (a) Poisson arrival (b) Limited service (c) Exponential service (d) Single server
- 14) The dead bodies coming to a burial ground is an example of _____. (a) Pure Birth Process (b) Pure death Process (c) Birth and Death Process (d) Constant rate of arrival
- 15) The system of loading and unloading of goods usually follows _____. (a) LIFO (b) FIFO (c) SIRO (d) SBP
- 16) A steady state exist in a queue if _____. (a) $\lambda > \mu$ (b) $\lambda < \mu$ (c) $\lambda \leq \mu$ (d) $\lambda \geq \mu$
- 17) Which of the following relation is not true:
(a) $L_s = L_q + \frac{1}{\lambda}$ (b) $L_s = \lambda W_s$ (c) $L_q = \lambda W_q$ (d) $W_s = W_q + \frac{1}{\mu}$

GATE

- 1) (a) Solution of Maximize $4x_1 + 6x_2 + x_3$, subject to $2x_1 - x_2 + 3x_3 \leq 5$; $x_1, x_2, x_3 \geq 0$ is _____ (b) Adding the constraint $x_2 \leq 2$, solution becomes _____. (GATE 2000)
- 2) A company places orders for supply of two items A and B. The order cost for each of the items is Rs.300/order. The inventory carrying cost is 18% of the unit price per year per unit. The unit prices of the items are Rs.40 and Rs.50 respectively. The annual demands are 10,000 and 20,000 respectively. (a) EOQ for item A is _____ (b) Thee minimum total cost for both items is _____ (c) A supplier is willing to give a 1% discount on



- price on item A, if the order quantities for each item are 1000 units or more. Is it profitable to avail the discount ____ (Specify Yes/No)? (GATE 2000)
- 3) In a single server infinite population queuing model, arrivals follow a Poisson distribution with mean $\lambda = 4$ per hour. The service times are exponential with mean service time equal to 12 minutes. The expected length of the queue will be _____. (a) 4 (b) 3.2 (c) 1.25 (d) 5 (GATE 2000)
 - 4) A company is offered the following price breaks for order quantity. If order quantity is between 0 – 100 then Price is Rs. 150 and Price is Rs. 100 for Order quantity above 100. Order cost is Rs.60 per order while the holding cost is 10% of the purchase price. If the annual requirement is 1000 units, EOQ = _____. (GATE 2001)
 - 5) A furniture manufacturer produces chairs and tables. The wood-working department is capable of producing 200 chairs or 100 tables or any proportionate combinations of these per week. The weekly demand for chairs and tables is limited to 150 and 80 units respectively. The profit from a chair is Rs.100 and that from a table is Rs.300. (a) The optimum product mix for maximizing the profit is _____ (b) The maximum profit is _____. (c) If the profit of each table drops to Rs.200 per unit, then the profit is _____. (GATE 2002).
 - 6) An item can be purchased for Rs.100. The ordering cost is Rs.200 and the inventory carrying cost is 10% of the item cost per annum. If the annual demand is 4000 units, the economic order quantity (in units) is: (a) 50 (b) 100 (c) 200 (d) 400 (GATE 2002).
 - 7) A company has introduced a new product with fixed cost of Rs.200 per week and unit variable cost of Rs.7. The product is sold to a retailer with a quantity discount as per the following schedule: Quantity 0 – 99 units then Unit price Rs.10 and for quantity 100 units onwards unit price is Rs.8. The range of quantities sold for the company to earn profit is _____? (GATE 2002).
 - 8) Arrivals at a telephone booth are considered to be Poisson, with an average time of 10 minutes between successive arrivals. The length of a phone call is distributed exponentially with mean 3 minutes. The probability that an arrival does not have to wait before service is _____. (a) 0.3 (b) 0.5 (c) 0.7 (d) 0.9 (GATE 2002).
 - 9) A manufacturer produces two types of products, 1 and 2, at production levels of x_1 and x_2 respectively. The profit is given is $2x_1 + 5x_2$. The production constraints are $x_1 + 3x_2 \leq 40$; $3x_1 + x_2 \leq 24$; $x_1 + x_2 \leq 10$; $x_1, x_2 \geq 0$. The maximum profit which can meet the constraints is (a) 29 (b) 38 (c) 44 (d) 75 (GATE 2003).
 - 10) Market demand for springs is 8, 00,000 per annum. A company purchases these springs in lots and sells them. The cost of making a purchase order is Rs.1, 200. The cost of storage of springs is Rs.120 per stored piece per annum. The economic order quantity is _____. (a) 400 (b) 2,828 (c) 4,000 (d) 8,000 (GATE 2003).
 - 11) A company produces two types of toys: P and Q. Production time of Q is twice that of P and the company has a maximum of 2000 time units per day. The supply of raw material is just sufficient to produce 1500 toys (of any type) per day. Toy type Q requires an electric switch which is available at 600 pieces per day only. The company makes a profit of Rs.3 and Rs.5 on type P and Q respectively. For maximization of profits, the daily production quantities of P and Q toys should respectively be: (a) 100, 500 (b) 500, 100 (c) 800, 600 (d) 1000, 1000 (GATE 2004).

IES

- 1) (IES 2008) Which one of the following statements is not correct? (a) A linear programming problem with 2 variables and 3 constraints can be solved by Graphical Method (b) In big-M method if the artificial variable cannot be driven out it depicts an



- optimal solution (c) Dual of a dual is the primal problem (d) For mixed constraints either big-M method or two phase method can be employed
- 2) (IES 2008) In order for a transportation matrix which has six rows and four columns not to degenerate, what is the number of occupied celled in the matrix?
(a) 6 (b) 9 (c) 15 (d) 24
 - 3) (IES 2008) In the basic EOQ model, if demand is 60 per month, ordering cost is Rs. 12 per order, holding cost is Rs. 10 per unit per month. What is the EOQ?
(a) 12 (b) 144 (c) 24 (d) 28
 - 4) (IES 2008) In the basic EOQ model, if lead time increases from 5 to 10 days, the EOQ will: (a) double (b) decrease by a factor of two (c) remain the same (d) The data is insufficient to find EOQ
 - 5) (IES 2008) The inter-arrival times at a tool crib are exponential with an average time of 10 minutes and the length of the service time is assumed to be exponential with mean 6 minutes. The probability that a person arriving at the booth will have to wait is equal to:
(a) 0.15 (b) 0.40 (c) 0.42 (d) 0.69
 - 6) (IES 2008) In a single server queuing system with arrival rate of ' λ ' and mean service time of ' μ ' the expected number of customers in the system is $\lambda/(\mu - \lambda)$. What is the expected waiting time per customer in the system?
(a) $\lambda^2/(\mu - \lambda)$ (b) $(\mu - \lambda)$ (c) $1/(\mu - \lambda)$ (d) $(\mu - \lambda)/\lambda$
 - 7) (IES 2009) While solving a linear simplex method, if all ratios of the right hand side to the coefficient in the key row become negative, then the problem has which of the following types of solution?
(a) An unbounded solution (b) Multiple solution (c) A unique solution (d) No solution
 - 8) (IES 2009) In a linear programming problem, which one of the following is correct for graphical method?
(a) A point in feasible region is not a solution to the problem
(b) One of the corner points of the feasible region is not the optimum solution
(c) Any point in the positive quadrant does not satisfy the non-negativity constraint
(d) The lines corresponding to different values of objective functions are parallel.
 - 9) (IES 2009) Which one of the following is true in case of simplex method of linear programming? (a) The constants of constraints equation may be positive or negative (b) Inequalities are not converted into equations (c) It cannot be used for two-variable problems (d) The simplex algorithm is an iterative procedure
 - 10) (IES 2009) A linear programming problem with mixed constraints (some constraints of \leq type and some of \geq type) can be solved by which of the following method? (a) Big-M method (b) Hungarian method (c) Branch and bound technique (d) Least cost method

Websites Addresses:

- 1) www.informs.org
- 2) <http://nptel.iitm.ac.in/video.php?subjectId=112106134>
- 3) <http://www.wikihow.com/Use-the-Hungarian-Algorithm>
- 4) http://www.youtube.com/watch?feature=player_embedded&v=BUGIhEecipE
- 5) http://canmedia.mcgrawhill.ca/college/olcsupport/stevenson/om3ce/IOM_applets/hungarianMethod/Hungarian.htm
- 6) www.scienceofbetter.org/



Expert Details:

- 1) Prof. M. Ram Mohan Rao, ISB, Hyderabad
- 2) Prof. Arza K. Rao, Secunderabad
- 3) Dr. N. V. S. Raju, Vice-Principal, JNTU-Jagtial
- 4) Dr. A. Rao, SVU, Tirupati
- 5) Dr. G. Padmanabhan, SVU, Tirupati
- 6) Dr Ravi Vadlamani, Institute for Development & Research in Banking Technology, Hyderabad
- 7) Dr V.N.Sastry, Professor, IDRBT, Hyderabad
- 8) Dr. N. Karmarkar, Fellow of Bell Laboratories
- 9) Dr. Kiran Seth, Associate Professor, IIT-Delhi
- 10) Dr. G. Srinivasan, Professor, IIT-Chennai

Journals (National & International):

- 1) Annals of Operations research
- 2) Computers and Industrial engineering
- 3) Computers and operations research
- 4) Decision sciences
- 5) Engineering Management
- 6) European Journal of Industrial Engineering
- 7) European Journal of Operational research
- 8) IIE transactions
- 9) INFOR
- 10) Informs

List of Topics for Student Seminars:

- 1) Introduction to Operation Research
- 2) Linear Programming Problem – Formulation & Graphical solution
- 3) Linear Programming Problem – Simplex method & Artificial variables techniques
- 4) Transportation Problem– Basic Feasible Solution methods & MODI method
- 5) Assignment Problem– Hungarian Algorithm & Traveling Salesman Problem
- 6) Flow Shop & Job Shop Sequencing
- 7) Replacement of items that deteriorate with time
- 8) Group Replacement
- 9) Theory of Games– Minimax (maximin) Criterion and Dominance Principle
- 10) Theory of Games– Graphical method

Case Studies / Small Projects:

- 1) Transportation Problem
- 2) Assignment Problem
- 3) Quadratic assignment problem
- 4) Traveling Salesman Problem
- 5) Travelling salesman problem with multiple objective
- 6) Vehicle Routing Problem
- 7) Replacement of Items that deteriorate with time
- 8) Replacement of Items that fail completely
- 9) Shortest Path Problem
- 10) Capital Budgeting Problem
- 11) Facility Location Problem

